

INVESTIGATIONS OF THE AXISYMMETRICAL  
CONFINED JET

by

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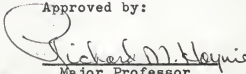
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## INTRODUCTION

The applications of the jet have been widely introduced in various engineering fields. For example, the jet water pump is one of them used in some Civil Engineering works such as deep-well pumping, booster pumping, dredging, tail water pumping and priming devices.

A jet boundary occurs between two streams which move at different speeds in the same general direction. Such a surface of discontinuity in the velocity of flow is unstable and gives rise to a zone of turbulent mixing downstream of the point where the two streams first meet. Some phenomena such as the width of the mixing region and the eddies existing in a jet are very important and of interest in practical applications. These phenomena are influenced by the velocity difference of the two streams.

As far as most engineers are concerned, high-velocity flow from a submerged outlet represents merely an irrecoverable loss of power, for a basic axiom of hydraulics states that the entire kinetic energy of such a jet will be dissipated through reactions with the surrounding fluid. The eddies generated by the velocity discontinuity between the jet and the surrounding fluid, will immediately result in a lateral mixing process which will proceed both inward and outward with distance from the efflux section. Such lateral mixing produces a necessarily balanced action and reaction.

Literature on the problems of jets has been in existence since about 1920, but few articles have been concerned with the confined jet. However, past studies of the jet in an infinite fluid provide considerable knowledge for this special type of jet. In general, the analysis of the mixing region in a jet is very complicated and the characteristics of the confined jet have not yet been fully established.

## THE PURPOSE OF THIS STUDY

The purpose of this study is to investigate the mixing process and the phenomena existing in the region of flow establishment of the confined jet. By utilizing dimensionless parameters, the mixing phenomena can be analyzed and a comparison may be made with the case of the jet in the infinite field.

## SCOPE OF THE STUDY

The experiments were conducted in this way; the jet was formed by issuing a flow from a 5/8" diameter steel pipe into a secondary flow which was flowing in the same direction in a 5" diameter plexiglas pipe. The jet was discharged along the central axis of the main pipe. The confined jet was axisymmetrical.

The velocities of both the jet and the secondary flow were varied from 0 to 16.269 ft/sec. for the jet and from 0 to 5.277 ft/sec. for the secondary flow. The total quantity of the discharge of these two streams varied from 0.014 to 0.721 cfs. Four series of runs were used for obtaining the data for this study. Each series consisted of a constant secondary flow with five or six runs of different velocities, from 0 to 16.269 ft/sec., for the jet.

In order to determine the magnitude of the velocity changes in the main pipe, the coordinate distribution method was used. The velocities for each run were measured at intervals of 1/2" along the vertical diameter of the cross section and each 4" along the pipe past the outlet of the jet.

## THEORY

Since it will be helpful for the further study of the confined jet, it is desirable to introduce some knowledge useful in the analysis for the case of a jet in an infinite field. The dimensional aspects of the phenomenon are first discussed, followed by the elementary physical analysis of the mean flow pattern.

### Jets In the Infinite Field

If the Reynolds number for the fluid efflux from a submerged boundary outlet is not too low, the mean velocity  $V$  at any point should depend only on the coordinates  $X, Y, Z$ , on the efflux velocity  $V_0$ , and on a linear dimension  $L_0$  characterizing the particular outlet form.

The dimensionless relationship of these variables may be grouped as

$$\frac{V}{V_0} = f_1 \left( \frac{X}{L_0}, \frac{Y}{X}, \frac{Z}{X} \right) \text{-----(1)}$$

The differential equation of continuity is

$$\frac{\partial V_x}{\partial X} + \frac{\partial V_y}{\partial Y} + \frac{\partial V_z}{\partial Z} = 0 \text{-----(2)}$$

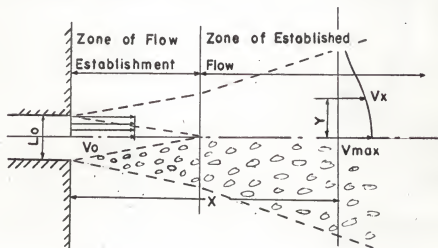


Figure 1. Schematic Representation of Jet Diffusion

The rate of flow  $Q$ , the momentum flux  $M$ , and the energy flux  $E$  past successive normal sections may be respectively written as the integral of the differential flux  $V_x dA$ ,  $(\rho V_x) V_x dA$  and  $(\rho V^2/2) V_x dA$  over any normal section.

Therefore, the following relations can be obtained

$$\frac{Q}{Q_0} = \frac{\int_0^\infty V_x dA}{V_0 A_0} = f_2 \left( \frac{X}{L_0} \right) \text{-----(3)}$$

$$\frac{M}{M_0} = \frac{\int_{-\infty}^{\infty} (V_x)^2 dA}{(V_0)^2 A_0} = f_3 \left( \frac{X}{L_0} \right) \text{-----} (4)$$

$$\frac{E}{E_0} = \frac{\int_{-\infty}^{\infty} V^2 V_x dA}{(V_0)^3 A_0} = f_4 \left( \frac{X}{L_0} \right) \text{-----} (5)$$

Where the subscript "o" indicates the quantity at the efflux cross section and the non subscripted quantity is any arbitrary section downstream of the efflux cross section.

For the case of the jet in the infinite field, the tangential shear force within the mixing region should decelerate the jet and accelerate the surrounding fluid. Since this process is wholly internal, it follows that the momentum flux must be a constant for all normal sections of a given flow pattern.

$$\frac{M}{M_0} = \frac{\int_{-\infty}^{\infty} (V_x)^2 dA}{(V_0)^2 A_0} = 1 \text{-----} (6)$$

Experimental data follow the general trend of the Gaussian normal probability function which is

$$\frac{V_x}{V_{\max}} = \exp \left( - \frac{Y^2}{2 \sigma^2} \right) \text{-----} (7)$$

where  $V_x$ ,  $V_{\max}$ ,  $Y$  and  $\sigma$  are as shown in Figure 2.

The use of eq. 7 in the analysis permits characteristics of the entire flow pattern to be expressed in terms of the two parameters which define the proportions of the curve; the velocity  $V_{\max}$  and the standard deviation  $\sigma$ .

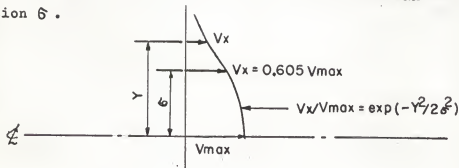


Figure 2 Characteristics of the Normal - Probability Curve  
Then Eq. (1) reduces to

$$\frac{V_{\max}}{V_0} = f_5 \left( \frac{X}{L_0} \right) \left( \frac{\sigma}{X} \right) \text{-----} (8)$$

The condition of dynamic similarity simultaneously requires that at any cross section, regardless of the efflux velocity

$$\frac{\delta}{X} = C \text{ -----(9)}$$

In other words, the angle of jet diffusion must be constant.

Based on the above general consideration, we make an assumption for the two-dimensional case such that

$$\frac{\delta}{X} = C_1 \text{ -----(10)}$$

Equation (6) of the momentum flux will lead to the expression

$$\frac{V_{\max}}{V_0} = \sqrt{\frac{1}{\pi} \frac{B_0}{C_1 X}} \text{ -----(11)}$$

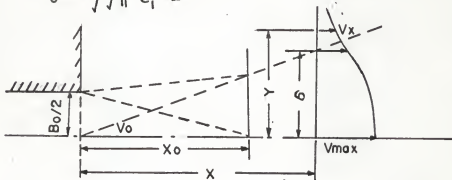


Figure 3 Definition Sketch for Zone of Flow Establishment

The distribution of the longitudinal velocity component in the zone of the established flow may then be written as

$$\frac{V_x}{V_0} = \sqrt{\frac{1}{\pi} \frac{B_0}{C_1 X}} \exp \left[ -\frac{1}{2(C_1)^2} \frac{Y^2}{X^2} \right] \text{ (12)}$$

$$\frac{Q}{Q_0} = \sqrt{2\pi} C_1 \frac{X}{B_0} \text{ -----(13)}$$

$$\frac{E}{E_0} = \sqrt{\frac{2}{3\pi} \frac{B_0}{C_1 X}} \text{ -----(14)}$$

For the three-dimensional case, we can replace  $Y$  and  $B_0$  by  $R$  and  $D_0$  and integrate over the corresponding areas. Then the equivalent expressions for the condition that  $\delta/X = C_2$  are

$$\frac{V_{\max}}{V_0} = \frac{1}{2C_2} \frac{D_0}{X} \text{ -----(15)}$$

$$\frac{V_x}{V_o} = \frac{1}{2C_2} \frac{D_o}{X} \exp \left[ -\frac{1}{2(C_2)^2} \frac{R^2}{X^2} \right] \text{-----(16)}$$

$$\frac{Q}{Q_o} = 4C_2 \frac{X}{D_o} \text{-----(17)}$$

$$\frac{E}{E_o} = \frac{1}{3C_2} \frac{D_o}{X} \text{-----(18)}$$

Under this analysis, Hunter Rouse (6) performed a very successful experiment in 1948 and obtained the following results;

For the two-dimensional case

$$C_1 = 0.109 \text{-----(19)}$$

$$\frac{V_{\max}}{V_o} \sqrt{\frac{X}{B_o}} = 2.28 \text{-----(20)}$$

$$\frac{Q}{Q_o} = 0.62 \sqrt{\frac{X}{B_o}} \text{-----(21)}$$

$$\frac{E}{E_o} = 1.86 \sqrt{\frac{B_o}{X}} \text{-----(22)}$$

For the three-dimensional case

$$C_2 = 0.081$$

$$\frac{V_{\max}}{V_o} \frac{X}{D_o} = 6.2 \text{-----(23)}$$

$$\frac{Q}{Q_o} = 0.32 \frac{X}{D_o} \text{-----(24)}$$

$$\frac{E}{E_o} = 4.1 \frac{D_o}{X} \text{-----(25)}$$

### Jets In the Finite Field

The primary assumption made for the jet in the infinite field was the constancy of momentum flux past successive sections. The condition of continuity was then satisfied by lateral flow from or to infinity. If the field of flow is finite, such lateral flow cannot occur at the outer limits. The discharge, instead of the momentum flux, past successive transverse sections must then be constant. The resultant change in momentum from section to section of the zone of diffusion requires that there be an accompanying pressure gradient.



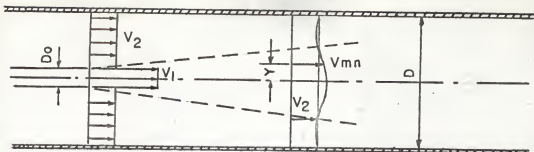


Figure 4 Flow from a Jet in the Bounded Region

For a jet in a bounded region, as shown in Figure 4 the outer limit of the zone of diffusion will be that radius at which the velocity is equal to  $V_2$ .

Although, from the experimental data (see Figure 9 to 13), the velocity profile in the central part of the conduit still has the property of the Gaussian normal probability function,

$$\frac{U_{mn}}{U_{max}} = \exp\left(\frac{-Y^2}{2\sigma^2}\right) \text{-----}(26)$$

the value of  $\sigma/X$  will not be a constant but will be determined by the effects of the pressure gradient. Since  $\sigma/X$  is not a function of the Gaussian normal probability function, the analysis used for the previous case of the free jet is not applicable.

However, the general consideration of Eq. (1), (2), (3), (4), and (5) are still satisfied if we replace all velocities by the relative velocities

$$U_{mn} = V_{mn} - V_2, U_{max} = V_{max} - V_2, U_0 = V_1 - V_2 \text{-----}(27)$$

and make the range of the integration extend from 0 to  $D/2$ .

By analogy to the case of the mixing of streams, one would expect that the jet would diffuse at smaller and smaller angles as the ratio of the velocities  $(V_1 - V_2)/V_1$  vary from 0 to 1. At the limit  $V_1 = V_2$ , the rate of spread resulting from shear-generated turbulence would be zero.

The discharge  $\int_0^{D/2} (V_x - V_2) 2\pi R dR$  past successive sections of the zone of diffusion must increase as the width of the zone increases. For an infinite field the increase in discharge would be supplied by

lateral inflow. For a finite field, if the ratio  $D/D_0$  is large but finite, an increase in jet discharge is characterized by a slight reduction of the velocity outside the zone of diffusion. If  $V_2$  is equal to zero, any reduction in the outside velocity obviously means a reverse flow from the diffusion jet to the area adjacent to the nozzle.

From the above discussion, the assumption of similarity must be retained also, but it may well require a different form than is used for the infinite field. Some dimensionless group relationships can be used to describe the above discussed phenomena.

#### REVIEW OF LITERATURE

In 1934, Kuethe (7) investigated the turbulent mixing regions formed by a plane jet and an axially symmetrical jet issuing into a fluid at rest and he also extended his investigation to consider the general case of the mixing of two parallel streams of different velocities. Velocity profiles in the mixing region of an axially symmetrical jet were measured by means of a pitot tube and good agreement was found between theory and experiment.

In 1948, Rouse (6) made some assumptions when he studied the diffusion of submerged jets and obtained analytical relationships. The measurements were shown to be in substantial agreement with the analytical relationships. He also provided the single experimental coefficient required to complete the analysis in the two-dimensional and in the three-dimensional cases. All results were reduced to a form immediately useful for design purposes for the flow of any liquid or gas at moderate to high Reynolds numbers.

In 1955, Weinstein, Osterle, and Forstall (8) studied the momentum diffusion from a slot jet into a moving secondary fluid. By introducing the correlation theory they concluded that the spreading coefficients for round and slot jets are independent of axial distances. This is analogous to results obtained for the case of a particle stream issuing from a point or line source into a field of homogeneous isotropic turbulence. Comparisons made between the slot jet and round jet diffusion processes indicate a relationship between the two mixing phenomena.

In 1964, Barchilon and Curtel (12), based on Craya's "Approximate confined jet theory" which is based on the Reynolds number and the continuity equations, studied the details of the structure of an axisymmetric confined jet with backflow. They used two experimental apparatuses in the investigation; one utilized water and the other air. The experimental results have made it possible to characterize the mean structure of the eddy in terms of the similitude parameter  $Ct$ .

In 1964, Mueller (13) published a paper dealing with the determination of the optimum dimensions of the water jet pump so that the best efficiency could be obtained. He introduced several water jet pumps used in civil engineering such as indicated above in the introduction. Recommendations for the design of water jet pumps were also given.

In 1962, Maczynoski (11) added the consideration of the pressure factor into his study of a round jet in an ambient co-axial stream. The theoretical analysis indicates that the spread of the profile can be described by a characteristic length scale. The experimental results showed that near the center of the jet the profiles of the flow follow the Gaussian form but that near the edge they fall off with distance somewhat more steeply <sup>than</sup> the Gaussian form and the variation of the lateral influx appears to be an important feature distinguishing jets with and without ambient streams.

## EXPERIMENTAL PROCEDURE

### Experimental Apparatus

A photograph of the experimental apparatus is presented in Figure 5, and the schematic diagram is shown in Figure 6. Two stilling tanks were used in this experiment; a 2'x5'x7' tank used at the upstream end and a 2½'x4'x2½' tank used at the downstream end. A 5" diameter plexi-glas pipe 6' in length, which connected these two tanks, was used for the main experiment.

Water was pumped from a reservoir and two water supply lines were used to make the jet and the secondary flow. Water for the jet with a velocity from 0 to 16.269 ft/sec. was passed through a 5/8" diameter hose and a 5/8" diameter steel pipe which was placed along the central axis of the main pipe. The jet was introduced at a distance of 1' downstream from the entrance of the main pipe. Water for the secondary flow with a velocity of 0 to 5.277 ft/sec. was supplied by a 4" diameter pipe. It flowed into the upstream stilling tank and was passed through the main pipe where it joined the jet. The mixed flow then proceeded downstream to the stilling tank where the total quantity was measured at the weir.

In order to avoid the effects of the oscillation and to get a uniform secondary flow, a double-level screen was placed beneath the outlet of the 4" water supply pipe and a bellmouth of 4" in curvature was fixed to the entrance of the main pipe.

A piezometer tube fastened along the upstream tank wall was used for the upstream water level reading. On the main pipe, four pitot-static tubes (see Figure 5) were spaced at 4" intervals from the outlet of the jet. They were used for measuring the velocities in the main pipe. The scales on the manometer tubes connected to the pitot tubes were graduated in increments of 0.001 ft.

A 7 7/16" x 9 1/2" rectangular weir was placed at the outlet of the downstream tank for measuring the total discharge. The reading of the water head at the weir was given by a point gage which was graduated in increments of 0.001' and was located at 1'-11" upstream from the weir.

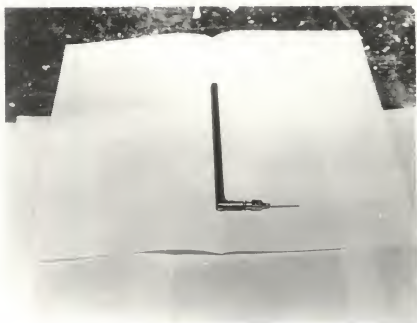


Fig. 5 The Pitot-static Tube Used in This Experiment

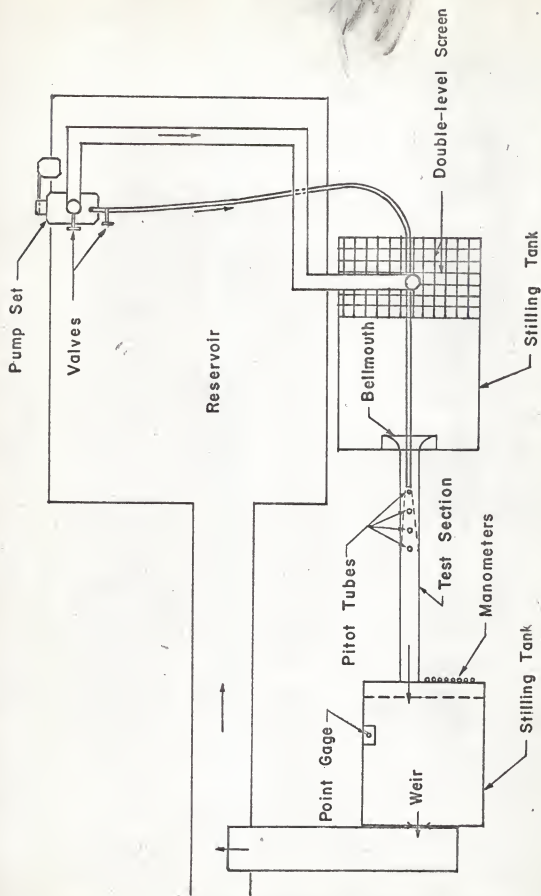


Fig. 6 Experimental Apparatus

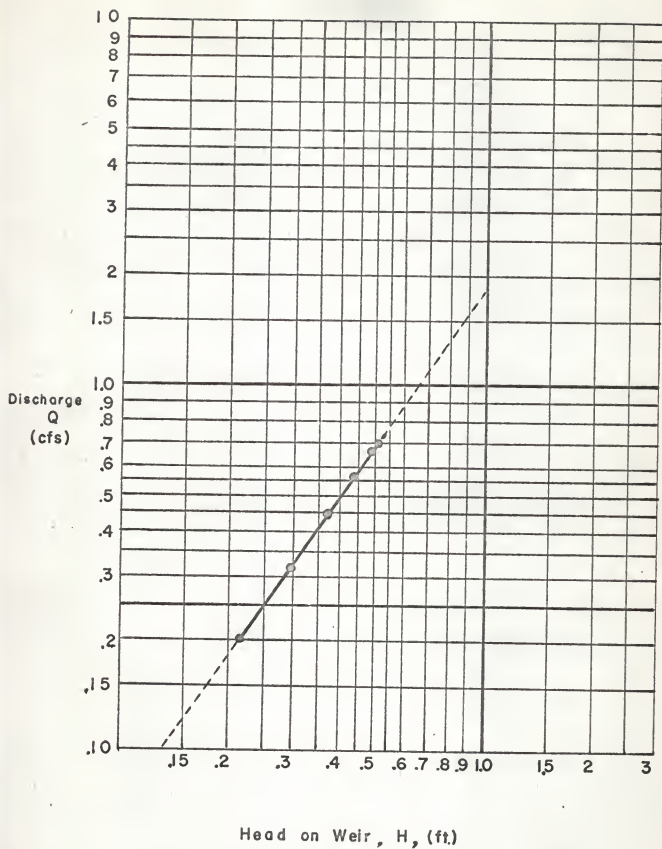


Fig.7 The Discharge Curve at the Weir

### Preliminary Experiments

There were two preliminary experimental procedures: the calibration of the weir; and, the determination of the coefficients of the pitot-static tubes. A rectangular weir was placed at the downstream reservoir outlet for determining the total discharge of the system.

The weir was calibrated over the range of flows. By timing the flow of a certain amount of water into a measuring tank and reading the corresponding head at the weir, the rate of flow could be calculated. The calibration curve is plotted as Figure 7.

After the weir was calibrated, coefficients of the pitot-static tubes were determined. The method of traversing the velocity profiles was used in this calibration. The head readings from the manometer were used to determine the velocity profile ( $V_p = \sqrt{2GH}$ ) and the mean of the integration of this profile gave the pitot-tube-measured mean velocity. Meanwhile, the head reading at the weir gave the real mean velocity in the pipe ( $V_m = Q/A$ ). Therefore, the coefficient of the pitot-static tube was  $K_m = V_p/V_m$ . Several different rates of flow were used for each pitot-static tube calibration. The calculations and the data are given in appendices III, IV, and V. The results show that the coefficients for pitot tubes 1, 2, 3, and 4, were respectively 0.986, 0.956, 0.932, and 0.961.

### Experiments For Obtaining Data

After the weir and the pitot tubes had been calibrated, the main part of the research followed. The experiments included four series of runs. The velocities of the secondary flow were kept nearly constant but the velocity of the jet was varied for each run in a series.

In the first series, the secondary flow was zero and the velocity of the jet was varied from 0 to 16.269 ft/sec. (five runs among this range). For each run, the water heads were read both at the head tank and at the downstream weir which was used to measure the quantity of flow. Meanwhile, each pitot tube was moved upward over the upper half diameter of the main pipe, and measured successively the velocities of each section at 0,



0.166, 0.333, 0.500, 1.000, 1.500, 2.000, and 2.475 inches from the central axis of the main pipe.

In the same manner, the velocity of the secondary flow was varied from 0 to 5.277 ft/sec. and the velocity of the jet was varied over the same range as above. The data collected in each run are given in Appendices IV and V.

## DATA ANALYSIS

### Method of Analysis

As mentioned above, the relationships among certain dimensionless groups can be used for the analysis of this experiment. The phenomena existing in the confined jet will be described and discussed.

The jet and the secondary flow are assumed to be uniform before they first meet. The experimental results (see Figures 9 to 13) show that this assumption is acceptable. All the analyses are based on the values of  $(V_1 - V_2)/V_1$  from 0 to 1.

The velocity of the jet for each run was obtained from the manometer reading of the head on the first pitot-static tube which was located directly in front of the nozzle of the jet. This velocity is expressed as

$$V_1 = K_1 \sqrt{2GH_1} \text{ ----- (28)}$$

where  $H_1$  is the velocity head reading on the pitot-static tube.

$K_1 = 0.986$ , is the coefficient of the pitot-static tube.

Therefore, the rate of jet flow will be

$$\begin{aligned} Q_1 &= (V_1) \cdot (A_0) \\ &= (K_1 \sqrt{2GH_1}) (D_0^2/4) \text{ ----- (29)} \end{aligned}$$

where  $D_0 = 5/8"$ , is the diameter of the jet nozzle.

The head reading at the weir and the calibration curve (Figure 6) give us the total discharge,  $Q$ , of the jet and the secondary flow. Then, the rate of the secondary flow will be

$$Q_2 = Q - Q_1 \text{ ----- (30)}$$

And the velocity of the secondary flow will be

$$\begin{aligned} V_2 &= Q_2 / (A - A_1) \\ &= Q_2 / (D^2 - D_1^2) / 4 \text{ ----- (31)} \end{aligned}$$

where  $D = 5"$ , is the diameter of the main pipe.

$D_1 = 11/16"$ , is the external diameter of the jet conduit.

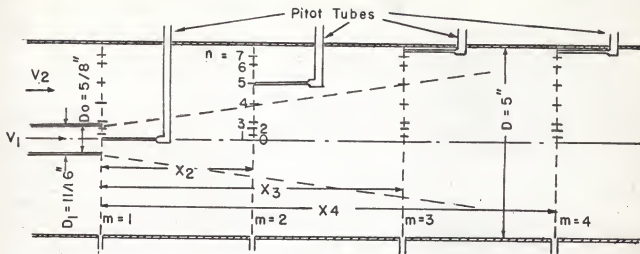


Figure 8 Zone of the velocity measurements

The velocities at the points of each section can be calculated if the manometer head readings are given (see Figure 8)

$$V_{mn} = K_m \sqrt{2GH_{mn}} \quad (32)$$

where  $m$  = cross sections 1, 2, 3, and 4.

$H_{mn}$  = the velocity head readings of the pitot-static tubes.

When all these velocities have been obtained, the following modified velocities can be determined;

$$U_{mn} = V_{mn} - V_2 \quad (33)$$

$$U_{max} = V_{max} - V_2 \quad (34)$$

$$U_0 = V_1 - V_2 \quad (35)$$

With the above values, the following dimensionless groups are obtained;

$$(R - D_0/2)/X$$

$$R/X$$

$$X/D_0$$

$$V_s$$

$$V_s$$

$$V_s$$

$$U_{mn}/U_0$$

$$U_{mn}/U_{max}$$

$$U_{max}/U_0$$

### Computation of Dimensionless Groups

All the experimental data were punched on IBM cards. The required computations were performed on the IBM 1620 Digital Computer. The flow diagrams are shown in Appendix III. All the input data have been printed in tabular form in Appendix IV and all the output data have been printed in Appendix V.

## DISCUSSION OF RESULTS

### Velocity Profiles

The case of the secondary flow equal to zero was studied first. It is evident, from Figure 9 that a negative velocity existed outside of the diffusion region. This phenomenon indicates that an adverse pressure gradient was present and that circulation occurred within this region. As discussed in the theory, this adverse pressure gradient must satisfy the change in momentum requirements. Comparing the two runs in Figure 9, it is seen that the circulation grows as the velocity difference ( $V_1 - V_2$ ) increases. The Gaussian normal function is not able to describe the whole velocity profile for this case, because of the existence of the circulation.

For the cases with non-zero secondary flow, all the velocity profiles, plotted at the section where the two streams first meet, indicate that the velocity of two streams are uniform, and the velocity profiles downstream from this section seem to change from section to section in a very reasonable manner. The Gaussian normal function appears to satisfy the region near the longitudinal axis of the pipe. Figures 10 through 13 indicate no reduction of the outside velocity due to the effects of the jet diffusion. However, the experimental data in Appendix V show that the phenomenon of the velocity reduction is present. There is no circulation evident in any of the runs having secondary flow, but it is believed that the circulation will occur if the velocity difference becomes very large. The plotted data indicate that the distance required for the establishment of mixing over the entire diameter of the pipe is proportional to the velocity difference. After the mixing has been completed, the flow will proceed downstream with a new modified profile.

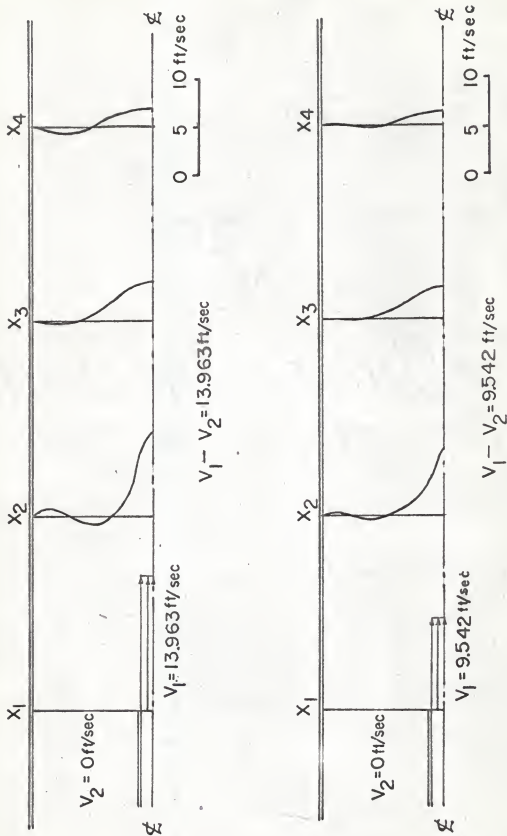


FIG. 9 VELOCITY PROFILES (A)

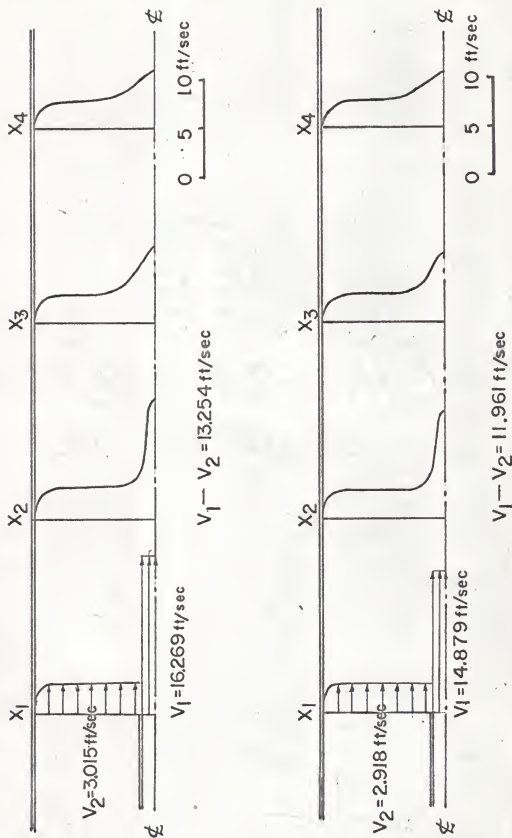


FIG. 10 VELOCITY PROFILES (B)

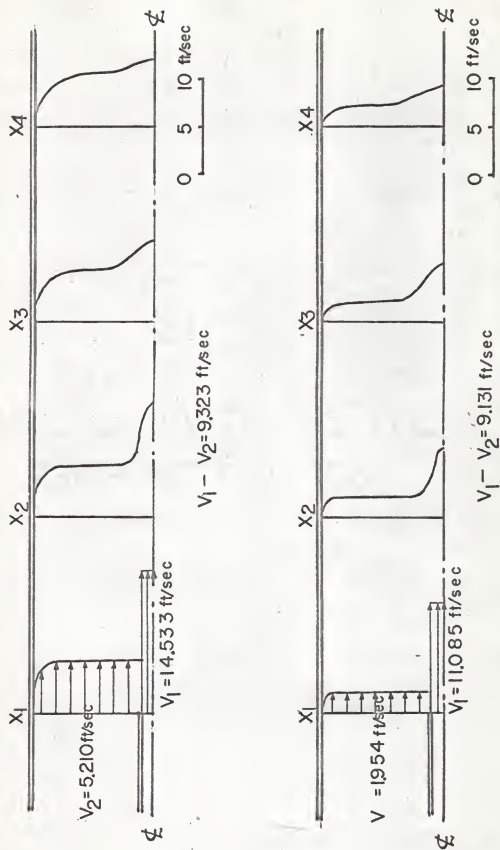


FIG. 11 VELOCITY PROFILES (C)



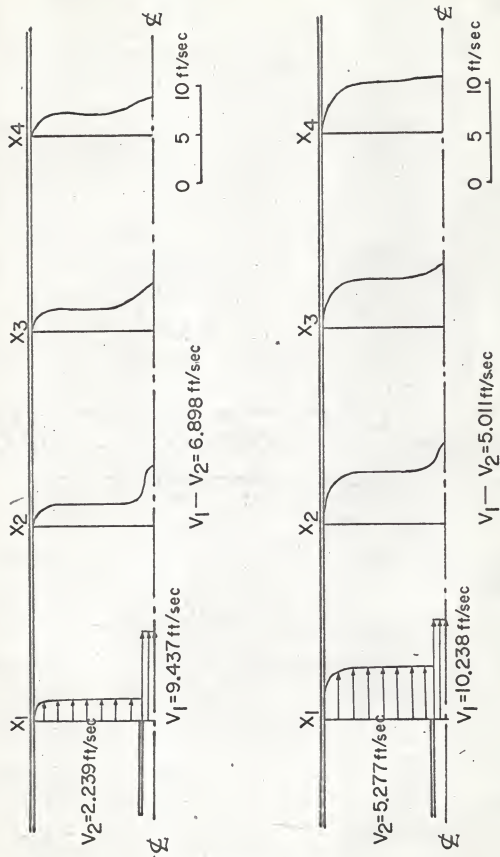


FIG. 12 VELOCITY PROFILES (D)

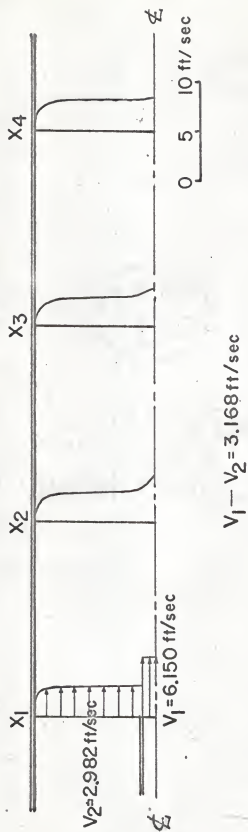


FIG. 13 VELOCITY PROFILES (E)

### Maximum Velocity Along the Central Axis

From Figures 14 and 15, it is seen that the maximum excess velocity in the jet is inversely proportional to the distance from the jet nozzle. As the jet moves downstream, the value of  $X/D_0$  increases and the curve changes gradually from a linear relationship to a non-linear relationship. For the case of the jet in an infinite field, the  $U_{\max}$ , based on the theoretical analysis, will approach zero as the distance  $X$  goes to infinity. For the jet in the finite field, since continuity must be maintained, the  $U_{\max}$  will approach a constant after the mixing process develops over the entire pipe cross section.

Figure 15 shows that the values of  $X/D_0$  at which the values of  $U_{\max}/U_0$  approach a constant is dependent on the value of  $(V_1 - V_2)/V_1$ . Obviously, as  $(V_1 - V_2)/V_1$  increases the value of  $X/D_0$  at which  $U_{\max}/U_0$  approaches a constant also increases. The value of  $U_{\max}/U_0$  for the case of  $(V_1 - V_2)/V_1 = 0.320$  is about 0.105. The curves in this figure suggest that all the final values of  $U_{\max}/U_0$  approach this value at some value of  $X/D_0$ .

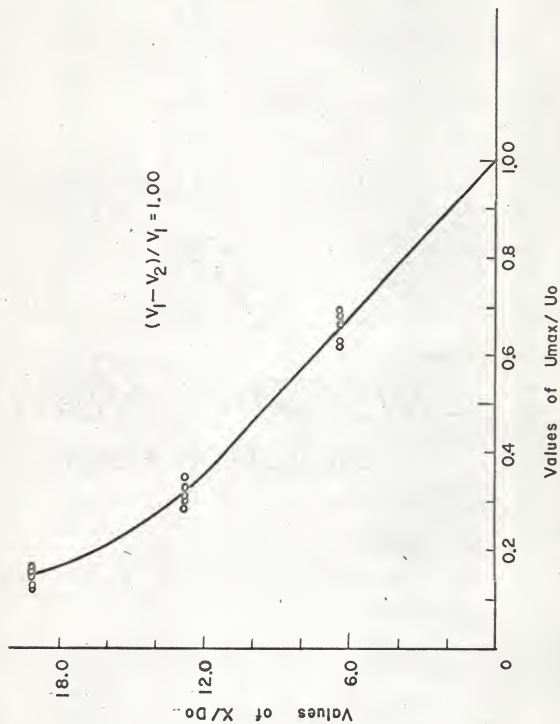


Fig.14 Distribution of Velocity Along the Central Axis (A)

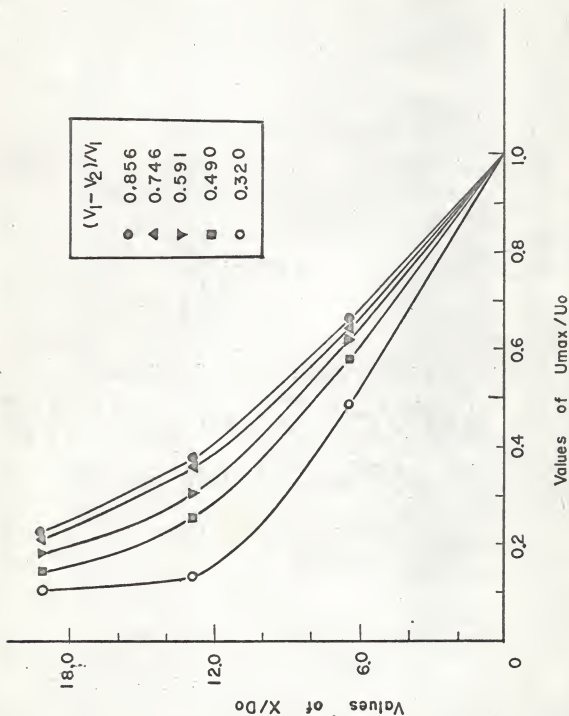


Fig. 15 Distribution of Velocity Along the Central Axis (B)

### The Velocity Phenomena Downstream of the Jet

As mentioned above, the experimental results show that an adverse pressure gradient exists in the region outside the diffusion zone.

Figures 16 thru 18 show the relationship of  $U_{mn}/U_{max}$  at given cross sections of the pipe and at various ratios of  $R/X$ . The value of  $U_{max}$  will be positive for all runs. Therefore, an adverse pressure gradient exists if the value of  $U_{mn}/U_{max}$  is negative. The values of  $R/X$  at the wall of the main pipe for the section  $X_2$ ,  $X_3$ , and  $X_4$  are respectively 0.630, 0.315, and 0.210. Some negative values of  $U_{mn}/U_{max}$  existed near the wall for each of the above cross sections, but the effects are considered to be due more to adhesion to the wall than to the pressure gradient.

The values of  $U_{mn}/U_{max}$  of most of the runs were positive at section  $X_2$  (Figure 16), since the diffusion of the jet is still narrow when it passes this section and the flow carried from the outside stream is so small that it does not create an adverse pressure gradient. This situation has been changed by the time the flow reaches section  $X_3$ . At section  $X_3$  negative values of  $U_{mn}/U_{max}$  are present over a large range of  $R/X$  (see Figure 17). This indicates that there is an adverse pressure gradient existing in this region. When secondary flow is zero, this adverse pressure gradient will cause recirculation. As the jet moves downstream to section  $X_4$  (Figure 18), the value of  $U_{mn}/U_{max}$  becomes positive for most runs. This change illustrates that the adverse pressure gradient has disappeared and the mixing has been completed over the entire cross section. The flow will proceed downstream with a new modified velocity profile. The effects of the jet will decrease as the flow moves downstream.

Another dimensionless group, based on the values of  $U_{mn}/U_0$  (Figure 19 thru 24), have been used to describe how the velocity profile for each run changes as the flow moves downstream. These curves show the same phenomena observed above; the largest adverse pressure gradient occurs at section  $X_3$  and disappears at section  $X_4$ . The adverse pressure gradient exists only in the zone where mixing is present.

The value of  $U_{mn}/U_0$  is always positive as long as the value of  $(R-D_0/2)/X$  is less than zero. It is found that no adverse pressure gradient exists near the central axis. At section  $X_3$  the region of adverse pressure gradient moves nearer the central axis as the values of  $(V_1-V_2)/V_1$  become smaller.

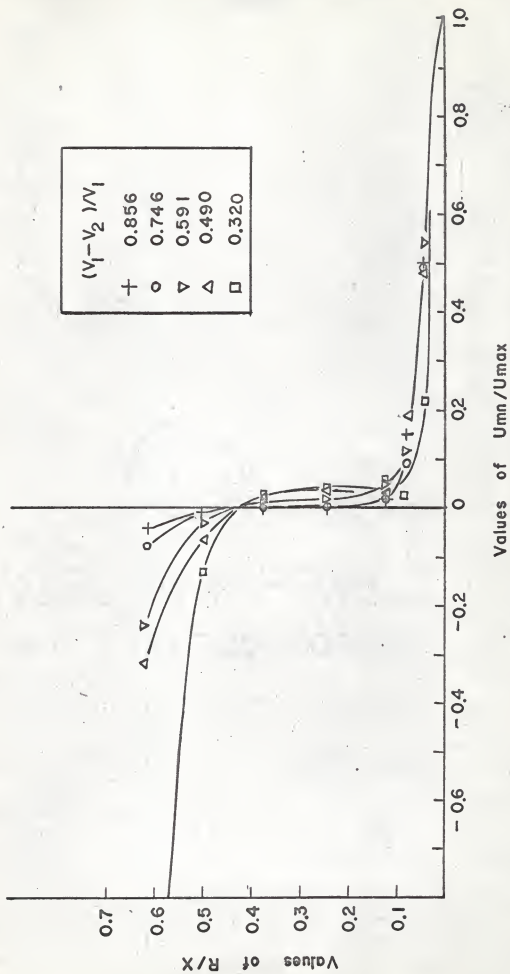


Fig. 16 Distribution of Velocity Characteristics in Flow (At  $X_2$ )



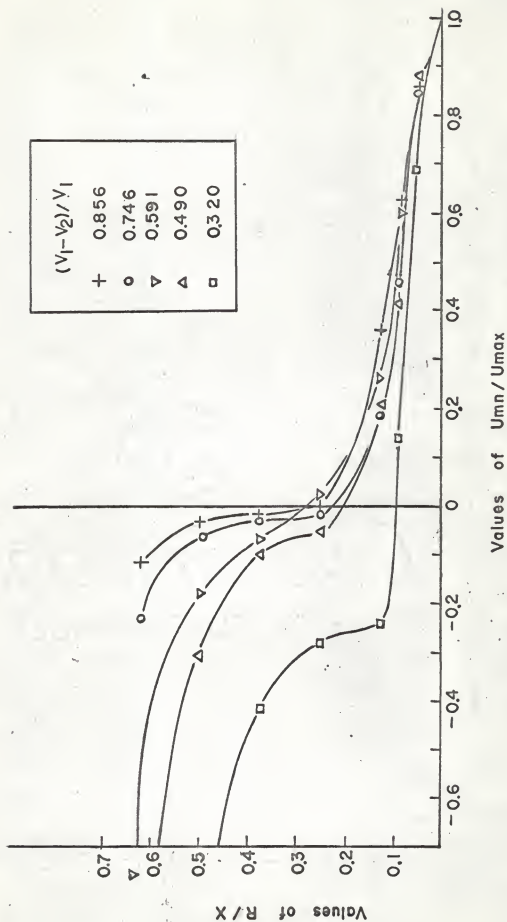
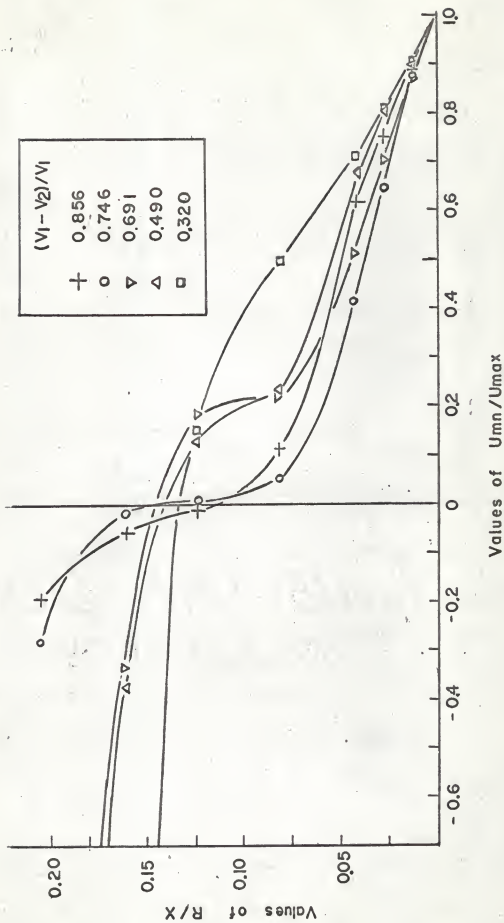


Fig. 17 Distribution of Velocity Characteristics in Flow (At  $X_3$ )

Fig. 18 Distribution of Velocity Characteristics in Flow (At  $X_4$ )

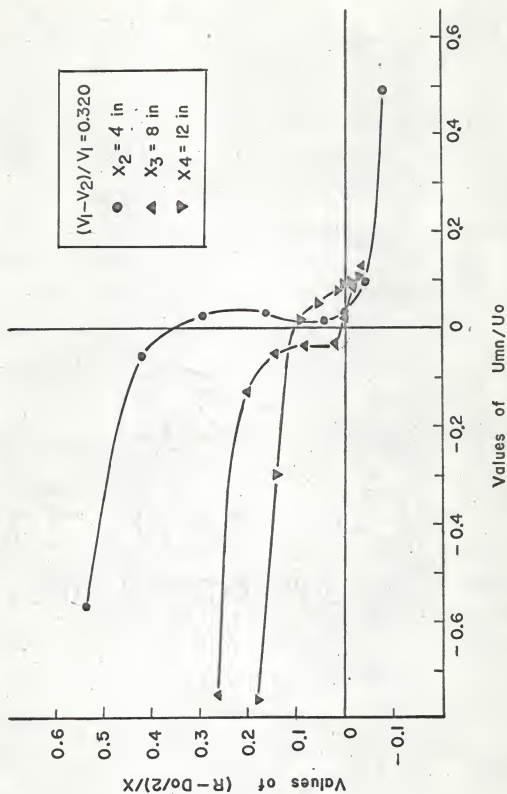


Fig. 19 Distribution of Longitudinal Velocity of Flow from Orifice (A)

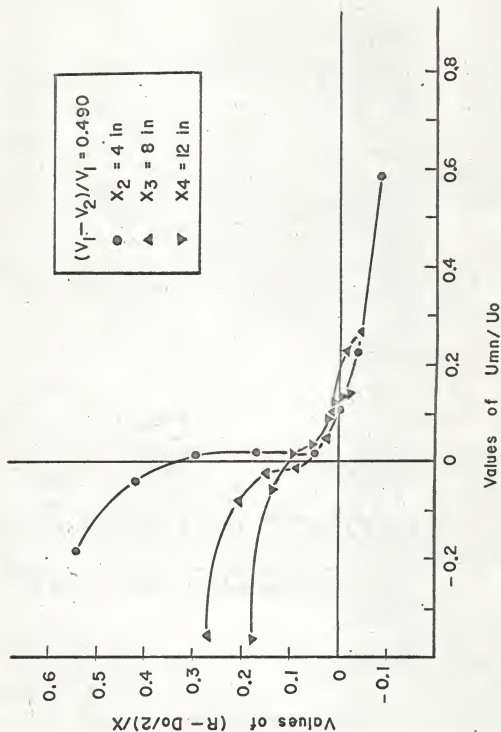


Fig 20 Distribution of Longitudinal Velocity of Flow from Orifice (B)

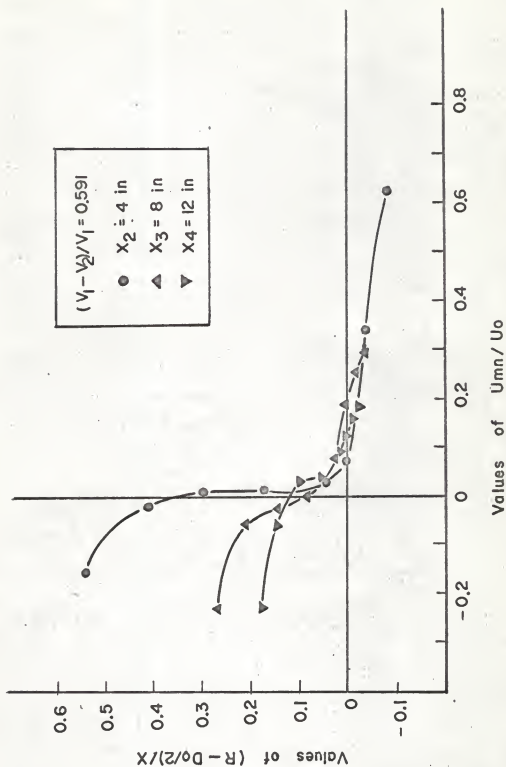


Fig. 21 Distribution of Longitudinal Velocity of Flow from Orifice (C)

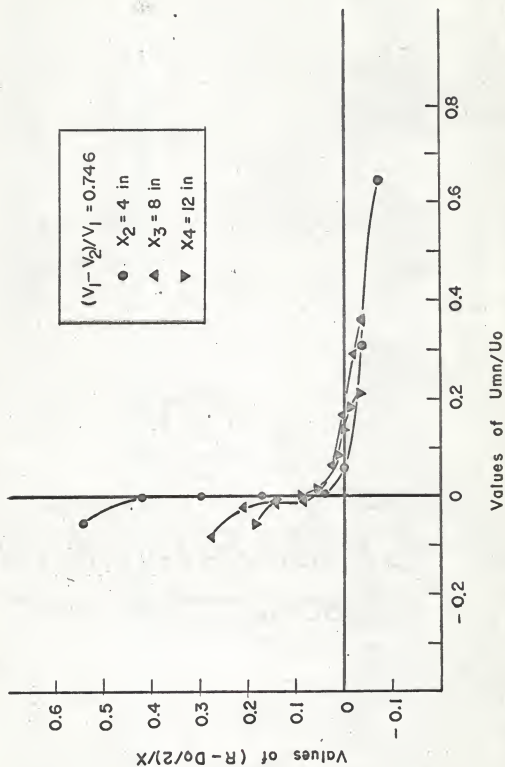


Fig. 2.2 Distribution of Longitudinal Velocity of Flow from Orifice (D)

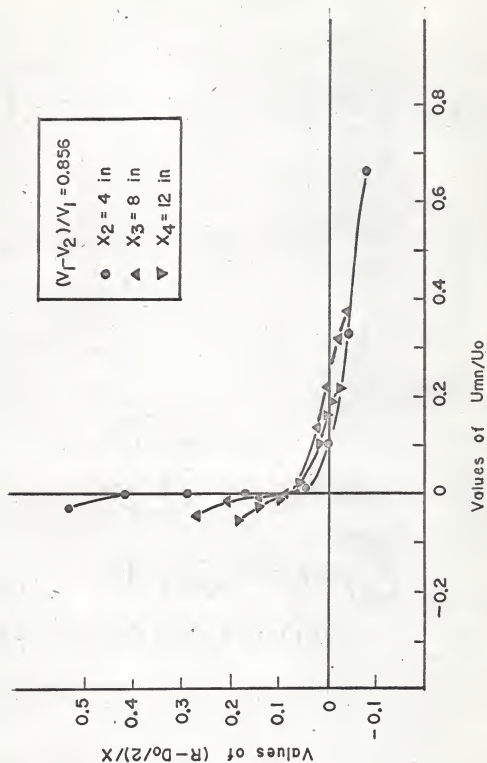


Fig 23 Distribution of Longitudinal Velocity of Flow from Orifice (E)

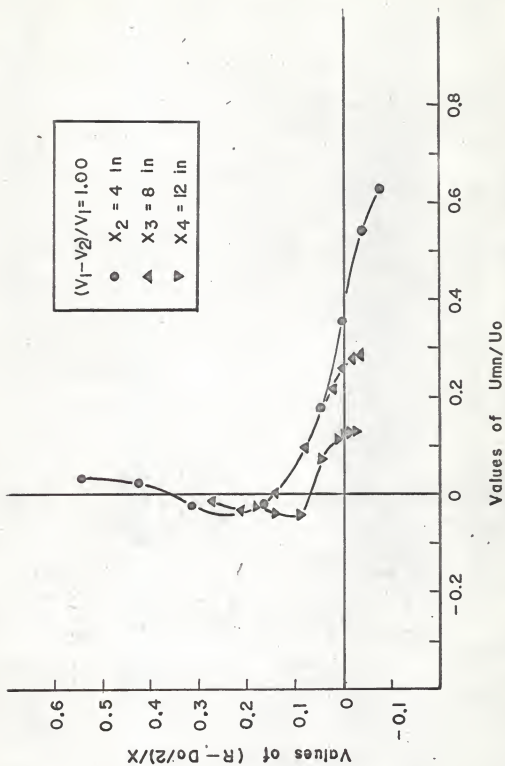


Fig. 24 Distribution of Longitudinal Velocity of Flow from Orifice (F)



## CONCLUSIONS

The characteristics of the jet diffusion in the finite field are quite different from those of the jet in the infinite field. In general, the former case is more complicated.

It was found that the Gaussian function, which was used very successfully in the study of a free jet, can be used for only a small region in the central part of the velocity profile for the confined jet.

It was found that the experimental results could be analyzed by means of dimensionless parameters. The experimental results show that, in contrast to the case of the infinite field in which the mixing continues as long as there is flow and the mixing extends to infinity, the mixing of a confined jet is completed within a determinable distance after the jet and the secondary flow meet. The mixed flow will continue downstream with a fixed profile.

The fundamental theoretical difference between the case of the finite field and infinite field is that finite field flow must satisfy the condition of continuity rather than the constancy of the momentum flux which must be satisfied in the infinite field. As mentioned in the theory, the pressure gradient, which may be influenced by many factors, will play an important role in the confined jet study.

## RECOMMENDATIONS FOR FURTHER STUDY

The following are recommended as subjects for further investigation.

Since the difference of the velocities of two streams will influence the production of the adverse pressure gradient, the investigation of higher velocity jets is suggested. The higher the velocity of the jet the more pronounced will be the influence. For such an investigation, a more powerful jet resource is required.

The above idea of changing the velocity leads to another suggestion. If the direction of one of the streams is changed, the effects of the adverse pressure gradient will also change. Therefore, let two streams meet from converging directions.

In general, as the ratio  $D/D_0$  decreases, the reduction of the velocity outside the diffusion region will become more pronounced and reverse flow may occur (depending on the ratio  $V_2/V_1$ ). It is suggested that an investigation be made by changing the ratio  $D/D_0$ . If the ratio is near 1, the effects of the shear forces existing along the solid boundary should be considered. It may be possible to incorporate boundary layer theory in this case.

## ACKNOWLEDGMENTS

The author acknowledges the counsel, guidance and critical review given by the major instructor of this study, Dr. Richard M. Haynie, Department of Civil Engineering, Kansas State University. His encouragement and efforts made possible the completion of this investigation.

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Acknowledgment is also given to Professor John E. Kipp and Dr. S. Thomas Parker for being on the advisory committee and reviewing the manuscript.

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## APPENDICES

## APPENDIX I

## TABLE OF NOMENCLATURE

A	: cross sectional area of the main pipe
A <sub>0</sub>	: cross sectional area of the jet nozzle
A <sub>1</sub>	: area of the outside cross section of the steel pipe
B <sub>0</sub>	: the width of the jet nozzle for two-dimensional case
C	: the constant of jet diffusion in the infinite field
C <sub>1</sub>	: the value of C for the two-dimensional case
C <sub>2</sub>	: the value of C for three-dimensional case
D	: the inside diameter of the main pipe
D <sub>0</sub>	: the inside diameter of the jet nozzle
D <sub>1</sub>	: the outside diameter of the jet conduit
E	: the energy flux at any section
E <sub>0</sub>	: the energy flux at the efflux section
G	: the acceleration of gravity of the earth, 32.2 ft/sec <sup>2</sup>
H <sub>n</sub>	: the head reading of the n <sup>th</sup> . point on the piezometer
HD	: the water level reading at the downstream tank
HU	: the water level reading at the head tank
HW	: the head reading at the weir, HW=HD-2.251'
HWL	: the water level difference between upstream and downstream tanks
H <sub>1</sub>	: the heading reading of the jet nozzle on the pitot-static tube
K <sub>m</sub>	: the coefficient of the m <sup>th</sup> pitot tube, m= 1, 2, 3, and 4
L <sub>0</sub>	: a linear dimension characterizing the particular outlet form
M	: the momentum flux at any section
M <sub>0</sub>	: the momentum flux at the efflux section
Q	: the rate of total flow
Q <sub>0</sub>	: the rate of flow at the efflux section
Q <sub>1</sub>	: the rate of jet flow
Q <sub>2</sub>	: the rate of the secondary flow
R	: the radial distance from the longitudinal central axis
T	: the temperature of the water
U <sub>max</sub>	: the modified maximum velocity, U <sub>max</sub> =V <sub>max</sub> -V <sub>2</sub>
U <sub>0</sub>	: the modified efflux velocity, U <sub>0</sub> = V <sub>1</sub> -V <sub>2</sub>

- $U_{mn}$  : the modified velocity,  $U_{mn} = V_{mn} - V_2$   
 $V$  : mean velocity at any point in flow  
 $V_m$  : the mean velocity in the pipe used in the calibration of the pitot tube  
 $V_{max}$  : the maximum velocity at the central axis  
 $V_{mn}$  : the velocity at the  $n^{th}$  point of the  $m^{th}$  section  
 $V_x$  : mean velocity in X direction  
 $V_o$  : the efflux velocity of the jet  
 $V_y$  : mean velocity in Y direction  
 $V_z$  : mean velocity in Z direction  
 $V_p$  : the pitot-tube-measured mean velocity used in the calibration of the pitot tube  
 $V_1$  : the velocity of the jet  
 $V_2$  : the mean velocity of the secondary flow  
 $X$  : the distance along the central axis from the jet  
 $Y$  : the coordinate distance in Y direction  
 $X_m$  : the sections of the velocity measurements,  $m = 1, 2, 3, \text{ and } 4$   
 $Z$  : the coordinate distance in Z direction  
 $\sigma$  : the deviation of the Gaussian normal function

## APPENDIX II

## FLOW DIAGRAMS USED FOR DIGITAL COMPUTER PROGRAM

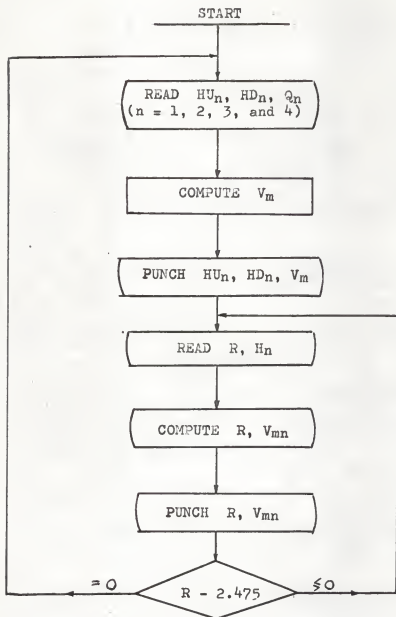


Fig. 25 The Determination of the Coefficients of pitot-static tubes



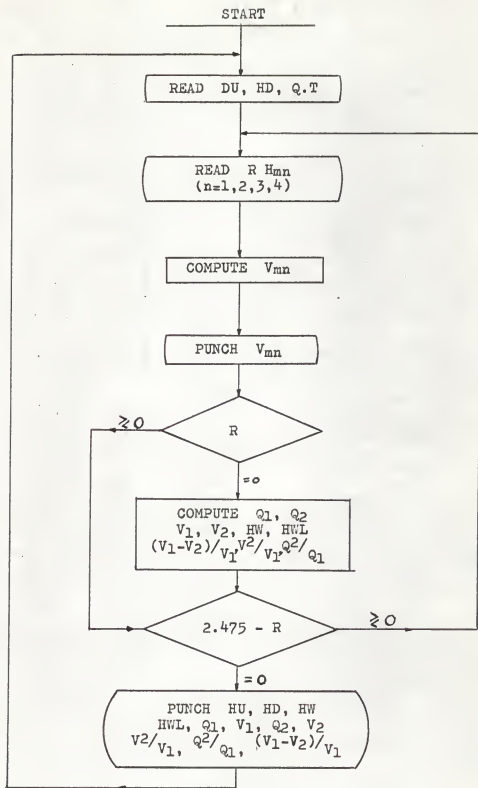
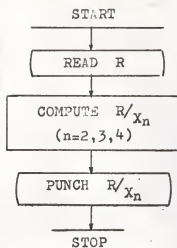


Fig. 26 The Calculation of the Fundamental Values of velocities, discharge, velocity ratio and discharge ratio.

(A)



(B)

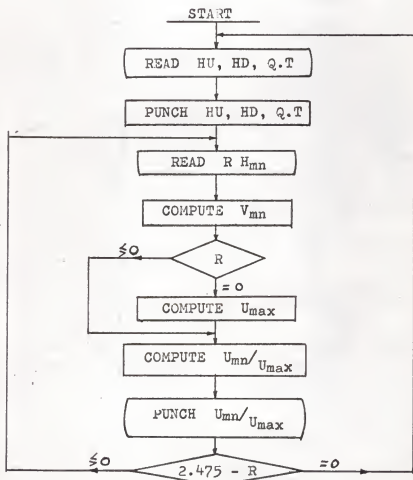


Fig. 27 The calculation of  $R/X$  and  $U_{mn}/U_{max}$

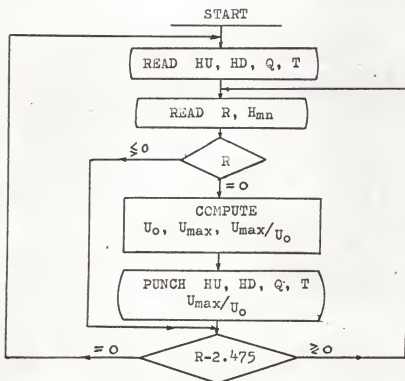
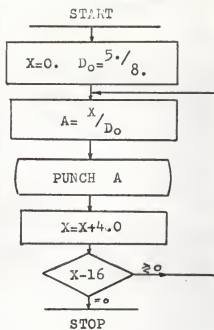


Fig. 28 The calculation of  $X/D_0$  and  $U_{\max}/U_0$

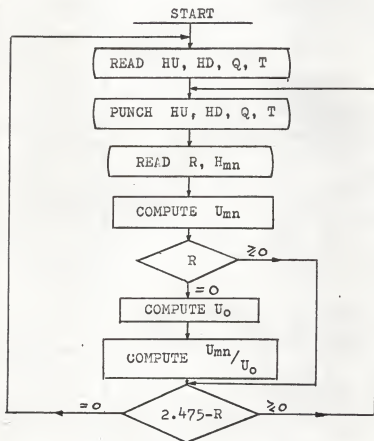
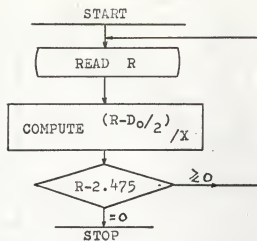


Fig. 29 The calculation of  $(R-D_0/2)/X$  and  $U_{mn}/U_0$

# APPENDIX III

## COMPUTER PROGRAMS USED FOR THIS STUDY

### C THE CALIBRATION OF THE COEFFICIENTS OF THE PITOT TUBES

```

101 READ 1,HU1,HU2,HU3,HU4
    READ 2,HD1,HD2,HD3,HD4
    READ 3,Q1,Q2,Q3,Q4
    V1=Q1/(3.1416*((15./12.)*2-(11./(16.*12.))*2)/4.))
    V2=Q2/(3.1416*((15./12.)*2/4.))
    V3=Q3/(3.1416*((15./12.)*2/4.))
    V4=Q4/(3.1416*((15./12.)*2/4.))
    PUNCH 4,HU1,HU2,HU3,HU4
    PUNCH 5,HD1,HD2,HD3,HD4
    PUNCH 6,Q1,Q2,Q3,Q4
    PUNCH 7,V1,V2,V3,V4
    PUNCH 9
102 READ 8,R,H1,H2,H3,H4
    U1=SQRT(2.*32.2*H1/12.)
    U2=SQRT(2.*32.2*H2/12.)
    U3=SQRT(2.*32.2*H3/12.)
    U4=SQRT(2.*32.2*H4/12.)
    PUNCH 10,R,U1,U2,U3,U4
    IF (2.475-R) 102,103,102
103 GC TC 101
    1 FCR4AT (F8.3,F8.3,F8.3,F8.3)
    2 FCRMAT (F8.3,F8.3,F8.3,F8.3)
    3 FCRMAT (F8.3,F8.3,F8.3,F8.3)
    4 FCRMAT (///5X4HHU1=F6.3,3X4HHU2=F6.3,3X4HHU3=F6.3,3X4HHU4=F6.3)
    5 FCRMAT (5X4HHD1=F6.3,3X4HHD2=F6.3,3X4HHD3=F6.3,3X4HHD4=F6.3)
    6 FCRMAT (6X3HQ1=F6.3,4X3HQ2=F6.3,4X3HQ3=F6.3,4X3HQ4=F6.3)
    7 FCRMAT (6X3HV1=F6.3,4X3HV2=F6.3,4X3HV3=F6.3,4X3HV4=F6.3)
    8 FCRMAT (F8.3,F8.3,F8.3,F8.3)
    9 FCRMAT (/53H R V1N V2N V3N V4N)
10 FCRMAT (3XF8.3,3XF8.3,3XF8.3,3XF8.3)
    EN

```

```

C C THE STUDY OF THE CONFINED JET (1)
101 READ 1,HU,HD,Q,T
    PUNCH 2
102 READ 3,R,H1,H2,H3,H4
    U1=0.986*SORT(2.*32.2*H1/12.)
    U2=0.956*SORT(2.*32.2*H2/12.)
    U3=0.932*SORT(2.*32.2*H3/12.)
    U4=0.961*SORT(2.*32.2*H4/12.)
    PUNCH 4,R,U1,U2,U3,U4
103 IF (R) 105,104,105
104 Q1=U1*(3.1416*(5./8./12.))**2/4.)
    Q2=Q-Q1
    V2=Q2/(3.1416/4.*(5./12.))**2-(11./(16.*12.))**2))
    A=V2/U1
    AA=(U1-V2)/U1
    V1=U1
    B=Q2/Q1
    HW=HD-2.251
    HWL=(HU-7.91)-12.*HW
105 IF (2.475-R) 102,106,102
106 PUNCH 5,HU,HD,HV,HV1,T
    PUNCH 6,Q1,V1,Q2,V2,Q
    PUNCH 7,A,B,AA
    GC TC 101
1 FORMAT (F8.3,F8.3,F8.3,F8.3) V1N V2N V3N V4N)
2 FORMAT (///51H R
3 FORMAT (F8.3,F8.3,F8.3,F8.3)
4 FORMAT (3XF6.3,5XF6.3,5XF6.3,5XF6.3)
5 FORMAT (3HHU=F6.3,4X3HHD=F6.3,4X3HHW=F6.3,4X4HHWL=F6.3,5X2HT=F5.2)
6 FORMAT (3H01=F6.3,4X3HV1=F6.3,4X3HQ2=F6.3,5X3HV2=F6.3,5X2HQ=F6.3)
7 FORMAT (6HV2/V1=F8.3,4X6HQ2/Q1=F8.3,4X11H(V1-V2)/V1=F8.3)
    EN

```

## C C THE STUDY OF THE CONFINED JET (2A)

```

101 PUNCH 1
    READ 2,HU,HD,Q,T
    PUNCH 3
102 READ 4,R,H1,H2,H3,H4
    RX2=R/4.
    RX3=R/8.
    RX4=R/12.
    PUNCH 5,R,RX2,RX3,RX4
103 IF (R-2.475) 102,104,102
104 STOP
    1 FORMAT (I27H THE CALCULATION OF R/X)
    2 FORMAT (F8.3,F8.3,F8.3,F8.3)
    3 FORMAT (I49H R R/X1 R/X2 R/X3 R/X4)
    4 FORMAT (F8.3,F8.3,F8.3,F8.3,F8.3)
    5 FORMAT (3XF6.3,13XF6.3,5XF6.3)
    END

```

## C C THE STUDY OF THE CONFINED JET (3A)

```

101 PUNCH 1
    X=0.
    D0=5./8.
102 A=X/D0
    PUNCH 2,A
    X=X+4.
    IF (X-16.) 102,103,102
103 STOP
    1 FORMAT (I27H THE CALCULATION OF X/D0)
    2 FORMAT (5XF8.3)
    END

```

C C THE STUDY OF THE CONFINED JET. (4A)

```

101 PUNCH 1
    PUNCH 2
102 READ 3,R
    RXD2=(R-5./16.)/4.
    RXD3=(R-5./16.)/8.
    RXD4=(R-5./16.)/12.
    PUNCH 4,R,RXD2,RXD3,RXD4
103 IF (R-2.475) 102,104,102
104 STOP
    1 FORMAT (/33H THE CALCULATION OF (R-D0/2)/X)
    2 FORMAT (/48H R X1 X2 X3 X4)
    3 FORMAT (F8.3)
    4 FORMAT (3XF6.3,13XF6.3,5XF6.3,5XF6.3)
END

```



```

C C THE STUDY OF THE CONFINED JET (2B)
  PUNCH 1
101 READ 2*HU,HD,Q,T
  PUNCH 3*HU,HD,Q,T
  PUNCH 5
102 READ 4*R,H1,H2,H3,H4
    U1=0.986*SQRT(2.*32.2*H1/12.)
    U2=0.956*SQRT(2.*32.2*H2/12.)
    U3=0.932*SQRT(2.*32.2*H3/12.)
    U4=0.961*SQRT(2.*32.2*H4/12.)
103 IF (R) 105,104,105
104 Q1=U1*(3.1416*(5./8./12.))*2/4.)
    Q2=Q-Q1
    V2=J2/(3.1416/4.*(5./12.))*2-(11./(16.*12.))*2))
    UM1=U1-V2
    UM2=U2-V2
    UM3=U3-V2
    UM4=U4-V2
105 UU1=(U1-V2)/UM1
    UU2=(U2-V2)/UM2
    UU3=(U3-V2)/UM3
    UU4=(U4-V2)/UM4
  PUNCH 6*R,UU1,UU2,UU3,UU4
  IF (2.475-R) 102,106,102
106 GC TO 101
      THE CALCULATION OF UMN/MAX)
  1 FORMAT (/32H
  2 FORMAT (F8.3,F8.3,F8.3,F8.3)
  3 FORMAT (/3X3HUU=F6.3,4X3HHD=F6.3,4X2HQ=F6.3,4X2HT=F5.2)
  4 FORMAT (F8.3,F8.3,F8.3,F8.3)
  5 FORMAT (/51H      R      U1N/UMAX      U2N/UMAX      U3N/UMAX      U4N/UMAX)
  6 FORMAT (3XF6.3,3XF6.3,4XF6.3,4XF6.3,4XF6.3)
  END

```

```

C C THE STUDY OF THE CONFINED JET (3B)
  PUNCH 1
101 READ 2,HU,HD,Q,T
102 READ 3,R,H1,H2,H3,H4
  IF (R) 105,110,105
110 U1=0.986*SQRT(2.*32.2*H1/12.)
  U2=0.956*SQRT(2.*32.2*H2/12.)
  U3=0.932*SQRT(2.*32.2*H3/12.)
  U4=0.961*SQRT(2.*32.2*H4/12.)
104 Q1=U1*(3.1416*(5./8./12.))*2/4.)
  Q2=Q-Q1
  V2=Q2/13.1416/4.*(5./12.)*2-(11./(16.*12.))*2))
  UM1=U1-V2
  UM2=U2-V2
  UM3=U3-V2
  UM4=U4-V2
  UM01=UM1/UM1
  UM02=UM2/UM1
  UM03=UM3/UM1
  UM04=UM4/UM1
  PUNCH 4,HU,HD,Q,T
  PUNCH 5
  PUNCH 6, UM01,UM02,UM03,UM04
105 IF (R-2.475) 102,106,102
106 GO TO 101
  1 FORMAT (/30H THE CALCULATION OF UMAX/UO)
  2 FORMAT (F8.3,F8.3,F8.3,F8.3)
  3 FORMAT (F8.3,F8.3,F8.3,F8.3,F8.3)
  4 FORMAT (/3HHU=F6.3,4XHHD=F6.3,4XH2HQ=F6.3,4XH2HT=F5.2)
  5 FORMAT (53HVALUE OF UMAX/UO AT X1 X2 X3 X4)
  6 FORMAT (25XF6.3,2XF6.3,2XF6.3,2XF6.3)
  END

```

```

C THE STUDY OF THE CONFINED JET (4B)
102 PUNCH 1
103 READ 2,HU,HD,O,T
PUNCH 3,HU,HD,Q,T
PUNCH 4
105 READ 5,R,H1,H2,H3,H4
U1=0.986*SQR(2.*32.2*H1/12.)
U2=0.956*SQR(2.*32.2*H2/12.)
U3=0.932*SQR(2.*32.2*H3/12.)
U4=0.961*SQR(2.*32.2*H4/12.)
110 IF (R) 115,111,115
111 O1=U1*(3.1416*(5./8./12.))*2/(4.)
O2=O-Q1
V2=Q2/13.1416/4.*(15./12.))*2-(11./(16.*12.))*2))
V0=U1-V2
115 UX1=U1-V2
UX2=U2-V2
UX3=U3-V2
UX4=U4-V2
VX01=UX1/V0
VX02=UX2/V0
VX03=UX3/V0
VX04=UX4/V0
PUNCH 6,R,VX01,VX02,VX03,VX04
IF (2.475-R) 105,125,105
125 GO TO 103

1 FORMAT (31H THE CALCULATION OF UMN/UO)
2 FORMAT (F8.3,F8.3,F8.3,F8.3)
3 FORMAT (///3X3HHU=F6.3,4X3HHO=F6.3,4X2HQ=F6.3,4X2HI=F5.2)
4 FORMAT (/53H R U1N/UO U2N/UO U3N/UO U4N/UO)
5 FORMAT (F8.3,F8.3,F8.3,F8.3)
6 FORMAT (3XF6.3,5XF6.3,5XF6.3,5XF6.3)
END

```

## APPENDIX IV

## INPUT DATA TO DIGITAL COMPUTER PROGRAM

## THE INPUT DATA FOR THE CALIBRATION OF PITCT TUBES

## SERIES (1)

HU1	HU2	HU3	HU4	
11.68	11.56	11.56	11.68	
HD1	HD2	HD3	HD4	
2.487	2.482	2.482	2.487	
Q1	Q2	Q3	Q4	
.230	0.223	0.223	0.230	
R	H1N	H2N	H3N	H4N
.000		0.54	0.54	0.60
.500	0.63	0.60	0.55	0.63
1.000	0.62	0.59	0.54	0.62
1.500	0.61	0.58	0.54	0.62
2.000	0.57	0.53	0.50	0.59
2.475	0.50	0.32	0.34	0.35

## SERIES (2)

HU1	HU2	HU3	HU4	
16.58	16.85	16.85	16.58	
HD1	HD2	HD3	HD4	
2.643	2.651	2.651	2.643	
Q1	Q2	Q3	Q4	
.480	0.492	0.492	0.480	
R	H1N	H2N	H3N	H4N
.000		2.40	2.59	2.68
.500	2.70	2.79	2.68	2.70
1.000	2.72	2.73	2.67	2.60
1.500	2.62	2.67	2.59	2.50
2.000	2.40	2.37	2.06	2.10
2.475	2.20	1.42	1.17	1.47

## SERIES (3)

HU1	HU2	HU3	HU4
20.22	19.97	19.97	20.22

HD1	HD2	HD3	HD4
2.726	2.719	2.719	2.726

Q1	Q2	Q3	Q4
.621	0.615	0.615	0.621

R	H1N	H2N	H3N	H4N
.000		3.79	4.02	4.37
.500	4.50	4.39	4.26	4.37
1.000	4.46	4.35	4.22	4.28
1.500	4.30	4.24	4.13	4.17
2.000	3.93	3.97	3.71	3.50
2.475	3.44	2.10	1.72	2.33

## THE INPUT DATA FOR THE MAIN STUDY

## SERIES (1)

HU	HD	Q	T	
7.500	2.299	0.033	23.0	
R	H1N	H2N	H3N	H4N
.000	47.00	19.25	4.80	0.90
.166		15.05	4.25	
.333		5.75	3.90	
.500	0.08	1.75	2.80	0.76
1.000	0.03	0.04	0.60	0.29
1.500	0.02	0.03	0.00	0.04
2.000	0.02	0.02	0.10	0.09
2.475	0.00	0.04	0.00	0.02

HU	HD	Q	T	
7.700	2.295	0.030	24.00	
R	H1N	H2N	H3N	H4N
.000	37.37	15.70	3.40	0.67
.166		12.00	3.20	
.333		4.90	2.65	
.500	0.04	1.25	1.90	0.52
1.000	0.02	0.03	0.41	0.23
1.500	0.02	0.02	0.00	0.08
2.000	0.02	0.02	0.05	0.06
2.475	0.02	0.05	0.01	0.02

HU	HD	Q	T	
7.820	2.289	0.024	25.1	
R	H1N	H2N	H3N	H4N
.000	25.08	13.05	2.75	0.70
.166		7.30	2.45	
.333		2.05	2.20	
.500	0.08	0.72	1.50	0.40
1.000	0.06	0.02	0.25	0.15
1.500	0.04	0.00	0.03	0.02
2.000	0.06	0.02	0.03	0.04
2.475	0.04	0.05	0.00	0.00

HU	HD	Q	T	
7.90	2.283	0.020	26.00	
R	H1N	H2N	H3N	H4N
.000	17.45	8.75	2.40	0.50
.166		4.00		
.333		1.85		
.500	0.03	0.41	1.40	0.33
1.000	0.03	0.02	0.25	0.06
1.500	0.01	0.02	0.02	0.01
2.000	0.03	0.02	0.00	0.02
2.475	0.01	0.00	0.00	0.00

HU	HD	Q	T	
8.000	2.275	0.014	26.5	
R	H1N	H2N	H3N	H4N
.000	8.57	4.06	1.05	0.20
.166		3.05		
.333		1.05		
.500	0.01	0.40	0.70	0.21
1.000	0.00	0.04	0.32	0.07
1.500	0.00	0.01	0.05	0.02
2.000	0.00	0.01	0.02	0.01
2.475	0.00	0.00	0.00	0.01

# SERIES (2)

HU	HD	Q	T	
11.80	2.523	0.283	17.5	
R	H1N	H2N	H3N	H4N
.000	40.35	20.90	9.65	4.55
.166		8.85	6.90	4.05
.333		2.64	3.90	2.49
.500	0.93	0.82	3.35	2.25
1.000	0.79	0.78	0.80	1.15
1.500	0.79	0.73	0.67	0.66
2.000	0.72	0.67	0.63	0.50
2.475	0.66	0.50	0.40	0.38

HU	HD	Q	T	
11.96	2.519	0.277	17.5	
R	H1N	H2N	H3N	H4N
.000	32.10	17.30	7.67	3.73
.166		6.08	6.45	3.30
.333		1.79	3.97	2.70
.500	0.87	0.81	2.39	1.90
1.000	0.82	0.74	0.75	0.93
1.500	0.79	0.71	0.69	0.68
2.000	0.74	0.67	0.65	0.55
2.475	0.67	0.48	0.41	0.34

HU	HD	Q	T	
12.25	2.525	0.285	17.5	
R	H1N	H2N	H3N	H4N
.000	23.55	11.92	6.70	3.40
.166		4.37	5.55	3.00
.333		1.42	4.09	2.60
.500	0.86	0.92	2.01	2.17
1.000	0.87	0.81	0.84	0.98
1.500	0.86	0.79	0.74	0.75
2.000	0.84	0.78	0.71	0.68
2.475	0.80	0.60	0.47	0.47

HU	HD	Q	T	
13.00	2.547	0.319	17.5	
R	H1N	H2N	H3N	H4N
.000	16.00	8.49	5.12	3.10
.166		3.90	4.20	2.83
.333		1.38	2.85	2.26
.500	1.08	1.18	2.14	1.92
1.000	1.12	1.06	1.10	1.23
1.500	1.08	1.05	1.04	1.05
2.000	1.06	1.03	1.04	1.01
2.475	1.03	0.78	0.65	0.63

HU	HD	Q	T	
13.45	2.557	0.333	17.5	
R	H1N	H2N	H3N	H4N
.000	8.66	4.86	3.39	2.15
.166		2.65	2.70	1.91
.333		1.67	1.90	1.77
.500	1.23	1.33	1.45	1.64
1.000	1.24	1.22	1.24	1.35
1.500	1.24	1.20	1.22	1.29
2.000	1.21	1.18	1.22	1.20
2.475	1.13	0.93	0.80	0.81



## SERIES (3)

HU	HD	Q	T	
14.87	2.620	0.438	19.8	
R	H1N	H2N	H3N	H4N
.000	50.73	30.42	13.43	7.58
.166		11.06	10.48	6.19
.333		3.15	6.23	5.06
.500	2.01	2.08	4.95	3.51
1.000	1.96	2.01	1.79	1.89
1.500	1.96	1.98	1.79	1.70
2.000	1.89	1.89	1.74	1.63
2.475	1.68	1.25	1.17	1.07

HU	HD	Q	T	
14.62	2.611	0.422	20.0	
R	H1N	H2N	H3N	H4N
.000	42.43	25.30	11.39	6.55
.166		11.15	9.05	5.68
.333		2.62	5.03	4.56
.500	1.91	1.81	3.19	3.43
1.000	1.85	1.75	1.68	1.81
1.500	1.83	1.74	1.66	1.63
2.000	1.78	1.72	1.61	1.53
2.475	1.70	1.33	1.03	0.87

HU	HD	Q	T	
14.79	2.610	0.420	20.4	
R	H1N	H2N	H3N	H4N
.000	33.60	20.00	9.57	5.46
.166		8.65	7.50	4.75
.333		2.72	4.59	3.61
.500	1.94	1.84	2.85	3.08
1.000	1.89	1.82	1.71	1.85
1.500	1.88	1.80	1.71	1.75
2.000	1.84	1.74	1.65	1.57
2.475	1.66	1.42	1.02	1.01

HU	HD	Q	T	
14.86	2.605	0.415	20.4	
R	H1N	H2N	H3N	H4N
.000	25.40	14.65	7.80	4.53
.166		6.35	6.32	4.14
.333		2.40	4.05	3.38
.500	1.91	1.81	2.62	2.72
1.000	1.88	1.78	1.75	1.83
1.500	1.81	1.77	1.72	1.73
2.000	1.77	1.72	1.62	1.69
2.475	1.63	1.26	1.04	1.17

HU	HD	Q	T	
14.98	2.607	0.416	21.0	
R	H1N	H2N	H3N	H4N
.000	15.59	9.64	5.53	3.25
.166		4.12	3.83	3.00
.333		2.03	3.12	2.56
.500	1.92	1.86	2.07	2.21
1.000	1.88	1.81	1.76	1.86
1.500	1.85	1.80	1.75	1.81
2.000	1.79	1.73	1.72	1.69
2.475	1.64	1.32	1.04	1.07

HU	HD	Q	T	
15.02	2.604	0.412	21.0	
R	H1N	H2N	H3N	H4N
.000	7.25	5.05	3.12	2.44
.166		2.58	2.75	2.24
.333		1.89	2.13	2.11
.500	1.93	1.86	1.95	1.95
1.000	1.91	1.85	1.84	1.89
1.500	1.84	1.83	1.81	1.89
2.000	1.82	1.76	1.79	1.83
2.475	1.66	1.32	1.13	1.59

## SERIES (4)

HU	HD	Q	T
22.60	2.777	0.728	21.0

R	H1N	H2N	H3N	H4N
.000	40.48	27.12	14.60	9.75
.166		21.95	14.02	9.62
.333		9.35	11.25	8.90
.500	5.31	6.05	8.25	7.50
1.000	5.66	5.78	5.84	6.10
1.500	5.66	5.61	5.56	5.50
2.000	5.30	5.35	4.95	4.32
2.475	4.65	3.12	2.42	2.39

HU	HD	Q	T
22.69	2.775	0.725	21.0

R	H1N	H2N	H3N	H4N
.000	31.16	20.10	12.00	8.75
.166		12.30	11.00	8.30
.333		6.74	9.45	7.70
.500	5.75	5.98	7.22	7.08
1.000	5.63	5.72	5.85	6.13
1.500	5.54	5.70	5.47	6.04
2.000	5.29	5.26	4.98	4.57
2.475	4.73	3.37	2.62	2.50

Q1	Q2	Q3	Q4
22.68	2.772	0.721	21.0

R	H1N	H2N	H3N	H4N
.000	20.09	13.54	9.15	7.10
.166		8.24	8.76	7.12
.333		6.80	7.15	6.78
.500	5.38	5.76	6.49	6.57
1.000	5.57	5.79	5.71	5.85
1.500	5.65	5.74	5.57	5.71
2.000	5.19	5.17	5.00	4.98
2.475	4.48	3.78	2.53	2.37

Q1	Q2	Q3	Q4
22.70	2.770	0.715	21.0

R	H1N	H2N	H3N	H4N
.000	11.30	8.40	6.58	6.08
.166		6.12	6.35	6.03
.333		5.42	5.95	5.97
.500	5.43	5.62	5.68	5.91
1.000	5.59	5.73	5.66	5.79
1.500	5.62	5.70	5.56	5.61
2.000	5.33	5.23	5.13	4.05
2.475	4.33	2.98	2.43	2.28

## APPENDIX V

## OUTPUT DATA FROM DIGITAL COMPUTER PROGRAM

## C C THE CALIBRATION OF THE COEFFICIENTS OF THE PITOT TUBES

HU1=11.680	HU2=11.560	HU3=11.560	HU4=11.680
HD1= 2.487	HD2= 2.482	HD3= 2.482	HD4= 2.487
Q1= .230	Q2= .223	Q3= .223	Q4= .230
V1= 1.719	V2= 1.635	V3= 1.635	V4= 1.687

R	VX1	VX2	VX3	VX4
.000	0.000	1.702	1.702	1.794
.500	1.839	1.794	1.718	1.839
1.000	1.824	1.779	1.702	1.824
1.500	1.809	1.764	1.702	1.824
2.000	1.749	1.687	1.638	1.779
2.475	1.638	1.310	1.351	1.371

VP1= 1.690	VP2= 1.560	VP3= 1.530	VP4= 1.610
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K1= .979	K2= .955	K3= .936	K4= .954
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HU1=16.580	HU2=16.850	HU3=16.850	HU4=16.580
HD1= 2.643	HD2= 2.651	HD3= 2.651	HD4= 2.643
Q1= .480	Q2= .492	Q3= .492	Q4= .480
V1= 3.588	V2= 3.608	V3= 3.608	V4= 3.520

R	VX1	VX2	VX3	VX4
.000	0.000	3.589	3.728	3.792
.500	3.807	3.869	3.792	3.807
1.000	3.821	3.828	3.785	3.735
1.500	3.750	3.785	3.728	3.663
2.000	3.589	3.566	3.325	3.357
2.475	3.436	2.761	2.506	2.809

VP1= 3.550	VP2= 3.470	VP3= 3.350	VP4= 3.380
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K1= .989	K2= .961	K3= .929	K4= .961
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HU1=20.220	HU2=19.970	HU3=19.970	HU4=20.220
HD1= 2.726	HD2= 2.719	HD3= 2.719	HD4= 2.726
Q1= .621	Q2= .615	Q3= .615	Q4= .621
V1= 4.642	V2= 4.510	V3= 4.510	V4= 4.554

R	VX1	VX2	VX3	VX4
.000	0.000	4.510	4.645	4.843
.500	4.914	4.854	4.781	4.843
1.000	4.892	4.832	4.759	4.793
1.500	4.804	4.770	4.708	4.731
2.000	4.592	4.616	4.462	4.334
2.475	4.297	3.357	3.038	3.536

VP1= 4.600	VP2= 4.300	VP3= 4.200	VP4= 4.400
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K1= .990	K2= .953	K3= .931	K4= .969
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# MEAN OF THE COEFFICIENTS

K1= .986	K2= .956	K3= .932	K4= .961
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## C C THE STUDY OF THE CONFINED JET (1)

## THE CALCULATION OF THE FUNDAMENTAL VALUES (SERIES 1)

R	V1N	V2N	V3N	V4N
.000	15.660	9.717	4.730	2.112
.166		8.592	4.451	
.333		5.311	4.264	
.500	.646	2.930	3.613	1.941
1.000	.396	.443	1.672	1.199
1.500	.323	.384	0.000	.445
2.000	.323	.313	.683	.668
2.475	0.000	.443	0.000	.315
HU= 7.500	HD= 2.299	HW= .048	HWL= -.986	T=23.00
Q1= .033	V1=15.660	Q2= 0.000	V2= 0.000	Q= .033
V2/V1= 0.000	Q2/Q1= 0.000	(V1-V2)/V1= 1.000		

R	V1N	V2N	V3N	V4N
.000	13.963	8.775	3.981	1.822
.166		7.672	3.862	
.333		4.902	3.515	
.500	.457	2.476	2.976	1.605
1.000	.323	.384	1.382	1.068
1.500	.323	.313	0.000	.630
2.000	.323	.313	.483	.545
2.475	.323	.495	.216	.315
HU= 7.700	HD= 2.295	HW= .044	HWL= -.738	T=24.00
Q1= .030	V1=13.963	Q2= 0.000	V2= 0.000	Q= .030
V2/V1= 0.000	Q2/Q1= 0.000	(V1-V2)/V1= 1.000		

R	V1N	V2N	V3N	V4N
.000	11.439	8.000	3.580	1.863
.166		5.984	3.379	
.333		3.171	3.202	
.500	.646	1.879	2.644	1.408
1.000	.560	.313	1.080	.862
1.500	.457	0.000	.374	.315
2.000	.560	.313	.374	.445
2.475	.457	.495	0.000	0.000
HU= 7.820	HD= 2.289	HW= .038	HWL= -.546	T=25.10
Q1= .024	V1=11.439	Q2= 0.000	V2= 0.000	Q= .024
V2/V1= 0.000	Q2/Q1= 0.000	(V1-V2)/V1= 1.000		

R	V1N	V2N	V3N	V4N
.000	9.542	6.551	3.345	1.574
.166		4.429		
.333		3.012		
.500	.396	1.418	2.555	1.279
1.000	.396	.313	1.080	.545
1.500	.228	.313	.305	.223
2.000	.396	.313	0.000	.315
2.475	.228	0.000	0.000	0.000
HU= 7.900	HD= 2.283	HW= .032	HWL= -.394	T=26.00
Q1= .020	V1= 9.542	Q2= 0.000	V2= 0.000	Q= .020
V2/V1= 0.000	Q2/Q1= 0.000	(V1-V2)/V1= 1.000		

R	V1N	V2N	V3N	V4N
.000	6.687	4.462	2.212	.996
.166		3.868		
.333		2.269		
.500	.228	1.401	1.806	1.020
1.000	0.000	.443	1.221	.589
1.500	0.000	.221	.483	.315
2.000	0.000	.221	.305	.223
2.475	0.000	0.000	0.000	.223
HU= 8.000	HD= 2.275	HW= .024	HWL= -.198	T=26.50
Q1= .014	V1= 6.687	Q2= 0.000	V2= 0.000	Q= .014
V2/V1= 0.000	Q2/Q1= 0.000	(V1-V2)/V1= 1.000		

# THE CALCULATION OF THE FUNDAMENTAL VALUES (SERIES 2)

R	V1N	V2N	V3N	V4N
.000	14.509	10.125	6.707	4.749
.166		6.588	5.671	4.480
.333		3.598	4.264	3.513
.500	2.081	2.005	3.952	3.339
1.000	2.030	1.956	1.931	2.387
1.500	2.030	1.892	1.767	1.809
2.000	1.938	1.813	1.714	1.574
2.475	1.856	1.566	1.366	1.372
HU=11.800	HD= 2.523	HW= .272	HWL= .626	T=17.50
Q1= .031	V1=14.509	Q2= .257	V2= 1.884	Q= .283
V2/V1= .130	Q2/Q1= 8.155	(V1-V2)/V1= .870		

R	V1N	V2N	V3N	V4N
.000	12.941	9.212	5.980	4.300
.166		5.461	5.483	4.044
.333		2.963	4.302	3.658
.500	2.131	1.993	3.338	3.069
1.000	2.068	1.905	1.870	2.147
1.500	2.030	1.866	1.793	1.836
2.000	1.965	1.813	1.741	1.651
2.475	1.870	1.534	1.382	1.298
HU=11.960	HD= 2.519	HW= .268	HWL= .834	T=17.50
Q1= .028	V1=12.941	Q2= .249	V2= 1.865	Q= .277
V2/V1= .144	Q2/Q1=	9.046	(V1-V2)/V1=	.856

R	V1N	V2N	V3N	V4N
.000	11.085	7.646	5.589	4.105
.166		4.630	5.086	3.856
.333		2.639	4.366	3.590
.500	2.118	2.124	3.061	3.279
1.000	2.131	1.993	1.979	2.204
1.500	2.118	1.968	1.857	1.928
2.000	2.093	1.956	1.819	1.836
2.475	2.043	1.715	1.480	1.526
HU=12.250	HD= 2.525	HW= .274	HWL= 1.052	T=17.50
Q1= .024	V1=11.085	Q2= .261	V2= 1.954	Q= .285
V2/V1= .176	Q2/Q1=	11.068	(V1-V2)/V1=	.824

R	V1N	V2N	V3N	V4N
.000	9.137	6.453	4.885	3.920
.166		4.374	4.425	3.745
.333		2.602	3.645	3.347
.500	2.374	2.406	3.158	3.085
1.000	2.417	2.280	2.264	2.469
1.500	2.374	2.269	2.202	2.281
2.000	2.352	2.248	2.202	2.237
2.475	2.318	1.956	1.741	1.767
HU=13.000	HD= 2.547	HW= .296	HWL= 1.538	T=17.50
Q1= .019	V1= 9.137	Q2= .300	V2= 2.239	Q= .319
V2/V1= .245	Q2/Q1=	15.388	(V1-V2)/V1=	.755



R	V1N	V2N	V3N	V4N	
.000	6.722	4.882	3.975	3.264	
.166		3.605	3.548	3.077	
.333		2.862	2.976	2.962	
.500	2.533	2.554	2.600	2.851	
1.000	2.544	2.446	2.404	2.587	
1.500	2.544	2.426	2.385	2.529	
2.000	2.513	2.406	2.385	2.439	
2.475	2.428	2.136	1.931	2.004	
HU=13.450	HD= 2.557	HW= .306	HWL= 1.868	T=17.50	
Q1= .014	V1= 6.722	Q2= .319	V2= 2.382	Q= .333	
V2/V1=	.354	Q2/Q1=	22.252	(V1-V2)/V1=	.646

## THE CALCULATION OF THE FUNDAMENTAL VALUES (SERIES 3)

R	V1N	V2N	V3N	V4N	
.000	16.260	12.215	7.912	6.120	
.166		7.265	6.990	5.539	
.333		3.931	5.389	5.008	
.500	3.238	3.194	4.804	4.171	
1.000	3.198	3.140	2.889	3.061	
1.500	3.198	3.116	2.889	2.903	
2.000	3.140	3.045	2.848	2.842	
2.475	2.961	2.476	2.335	2.303	
HU=14.870	HD= 2.620	HW= .369	HWL= 2.532	T=19.80	
Q1= .035	V1=16.269	Q2= .403	V2= 3.015	Q= .438	
V2/V1=	.185	Q2/Q1=	11.636	(V1-V2)/V1=	.815

R	V1N	V2N	V3N	V4N	
.000	14.879	11.140	7.287	5.698	
.166		7.395	6.495	5.306	
.333		3.585	4.842	4.754	
.500	3.157	2.980	3.856	4.123	
1.000	3.107	2.930	2.798	2.995	
1.500	3.090	2.921	2.782	2.842	
2.000	3.047	2.905	2.740	2.754	
2.475	2.978	2.554	2.191	2.077	
HU=14.620	HD= 2.611	HW= .360	HWL= 2.390	T=20.00	
Q1= .032	V1=14.879	Q2= .390	V2= 2.918	Q= .422	
V2/V1=	.196	Q2/Q1=	12.312	(V1-V2)/V1=	.804

R	V1N	V2N	V3N	V4N
.000	13.240	9.904	6.679	5.202
.166		6.514	5.913	4.852
.333		3.653	4.626	4.230
.500	3.181	3.004	3.645	3.907
1.000	3.140	2.988	2.823	3.028
1.500	3.132	2.971	2.823	2.945
2.000	3.098	2.921	2.773	2.789
2.475	2.943	2.639	2.181	2.237
HU=14.790	HD= 2.610	HW= .359	HWL= 2.572	T=20.40
Q1= .028	V1=13.240	Q2= .392	V2= 2.929	Q= .420
V7/V1=	.221	Q2/Q1=	13.889	(V1-V2)/V1= .779

R	V1N	V2N	V3N	V4N
.000	11.512	8.477	6.030	4.738
.166		5.581	5.428	4.530
.333		3.431	4.345	4.093
.500	3.157	2.980	3.495	3.672
1.000	3.132	2.955	2.856	3.012
1.500	3.073	2.946	2.832	2.928
2.000	3.039	2.905	2.748	2.894
2.475	2.916	2.486	2.202	2.408
HU=14.860	HD= 2.605	HW= .354	HWL= 2.702	T=20.40
Q1= .025	V1=11.512	Q2= .390	V2= 2.919	Q= .415
V7/V1=	.254	Q2/Q1=	15.921	(V1-V2)/V1= .746

R	V1N	V2N	V3N	V4N
.000	9.019	6.876	5.077	4.013
.166		4.495	4.225	3.856
.333		3.155	3.814	3.562
.500	3.165	3.020	3.106	3.310
1.000	3.132	2.980	2.864	3.036
1.500	3.107	2.971	2.856	2.995
2.000	3.056	2.913	2.832	2.894
2.475	2.925	2.544	2.202	2.303
HU=14.980	HD= 2.607	HW= .356	HWL= 2.798	T=21.00
Q1= .019	V1= 9.019	Q2= .397	V2= 2.966	Q= .416
V7/V1=	.329	Q2/Q1=	20.650	(V1-V2)/V1= .671

R	V1N	V2N	V3N	V4N
.000	6.150	4.977	3.814	3.478
.166		3.557	3.580	3.332
.333		3.045	3.151	3.234
.500	3.173	3.020	3.015	3.109
1.000	3.157	3.012	2.929	3.061
1.500	3.098	2.996	2.905	3.061
2.000	3.082	2.938	2.889	3.012
2.475	2.943	2.544	2.295	2.807
HU=15.020	HD= 2.604	HW= .353	HWL= 2.874	T=21.00
Q1= .013	V1= 6.150	Q2= .399	V2= 2.982	Q= .412
V2/V1= .485	Q2/Q1=	30.442	(V1-V2)/V1=	.515

## THE CALCULATION OF THE FUNDAMENTAL VALUES (SERIES 4)

R	V1N	V2N	V3N	V4N
.000	14.533	11.533	8.250	6.951
.166		10.376	8.084	6.905
.333		6.772	7.242	6.642
.500	5.264	5.447	6.201	6.097
1.000	5.434	5.324	5.218	5.498
1.500	5.434	5.246	5.091	5.221
2.000	5.259	5.123	4.804	4.627
2.475	4.926	3.912	3.359	3.442
HU=22.600	HD= 2.777	HW= .526	HWL= 8.378	T=21.00
Q1= .031	V1=14.533	Q2= .697	V2= 5.210	Q= .728
V2/V1= .359	Q2/Q1=	12.512	(V1-V2)/V1=	.641

R	V1N	V2N	V3N	V4N
.000	12.751	9.929	7.479	6.585
.166		7.767	7.161	6.414
.333		5.750	6.637	6.178
.500	5.477	5.416	5.801	5.924
1.000	5.420	5.297	5.222	5.512
1.500	5.376	5.287	5.040	0.000
1.500	5.376	5.287	5.050	5.471
2.000	5.254	5.079	4.818	4.759
2.475	4.968	4.066	3.495	3.520
HU=22.690	HD= 2.775	HW= .524	HWL= 8.492	T=21.00
Q1= .027	V1=12.751	Q2= .698	V2= 5.216	Q= .725
V2/V1= .409	Q2/Q1=	25.688	(V1-V2)/V1=	.591

R	V1N	V2N	V3N	V4N
.000	10.238	8.149	6.531	5.932
.166		6.957	6.390	5.940
.333		5.775	5.773	5.797
.500	5.298	5.315	5.500	5.706
1.000	5.391	5.329	5.159	5.385
1.500	5.429	5.306	5.096	5.320
2.000	5.204	5.036	4.828	4.968
2.475	4.835	4.306	3.434	3.427
HU=22.680	HD= 2.772	HW= .521	HWL= 8.518	T=21.00
Q1= .022	V1=10.238	Q2= .699	V2= 5.227	Q= .721
V2/V1= .510	Q2/Q1=	32.054	(V1-V2)/V1=	.490

R	V1N	V2N	V3N	V4N
.000	7.678	6.419	5.538	5.489
.166		5.479	5.441	5.467
.333		5.156	5.267	5.440
.500	5.323	5.250	5.146	5.412
1.000	5.401	5.301	5.137	5.357
1.500	5.415	5.287	5.091	5.273
2.000	5.273	5.065	4.890	4.480
2.475	4.753	3.823	3.366	3.362
HU=22.700	HD= 2.770	HW= .519	HWL= 8.562	T=21.00
Q1= .016	V1= 7.678	Q2= .699	V2= 5.222	Q= .715
V2/V1= .680	Q2/Q1=	42.707	(V1-V2)/V1=	.320

## C C THE STUDY OF THE CONFINED JET (2A)

THE CALCULATION OF  $R/X$ 

R	$R/X_1$	$R/X_2$	$R/X_3$	$R/X_4$
.000		0.000	0.000	0.000
.166		.042	.021	.014
.333		.083	.042	.028
.500		.125	.063	.042
1.000		.250	.125	.083
1.500		.375	.188	.125
2.000		.500	.250	.167
2.475		.619	.309	.206

## C C THE STUDY OF THE CONFINED JET (3A)

THE CALCULATION OF  $X/D_0$ 

VALUES AT  $X_2=6.400$   $X_3=12.800$   $X_4=19.200$

## C C THE STUDY OF THE CONFINED JET (4A)

THE CALCULATION OF  $(R-D_0/2)/X$ 

R	$X_1$	$X_2$	$X_3$	$X_4$
.000		-.078	-.039	-.026
.166		-.037	-.018	-.012
.333		.005	.003	.002
.500		.047	.023	.016
1.000		.172	.086	.057
1.500		.297	.148	.099
2.000		.422	.211	.141
2.475		.541	.270	.180

## C C THE STUDY OF THE CONFINED JET (28)

THE CALCULATION OF  $U_{MN}/U_{MAX}$  (SERIES 1)

HU= 7.500      HD= 2.299      Q= .033      T=23.00

R	$U_{1N}/U_{MAX}$	$U_{2N}/U_{MAX}$	$U_{3N}/U_{MAX}$	$U_{4N}/U_{MAX}$
.000	1.000	1.000	1.000	1.000
.166		.884	.941	
.333		.547	.901	
.500	.041	.302	.764	.919
1.000	.025	.046	.354	.568
1.500	.021	.040	.000	.212
2.000	.021	.033	.145	.317
2.475	.000	.046	.000	.150

HU= 7.700      HD= 2.295      Q= .030      T=24.00

R	$U_{1N}/U_{MAX}$	$U_{2N}/U_{MAX}$	$U_{3N}/U_{MAX}$	$U_{4N}/U_{MAX}$
.000	1.000	1.000	1.000	1.000
.166		.874	.970	
.333		.559	.883	
.500	.033	.282	.747	.881
1.000	.023	.044	.347	.585
1.500	.023	.035	.000	.345
2.000	.023	.035	.121	.299
2.475	.023	.056	.054	.172

HU= 7.820      HD= 2.289      Q= .024      T=25.10

R	$U_{1N}/U_{MAX}$	$U_{2N}/U_{MAX}$	$U_{3N}/U_{MAX}$	$U_{4N}/U_{MAX}$
.000	1.000	1.000	1.000	1.000
.166		.748	.944	
.333		.397	.895	
.500	.057	.235	.739	.756
1.000	.049	.039	.302	.464
1.500	.040	.000	.105	.170
2.000	.049	.039	.105	.240
2.475	.040	.062	.000	.001

HU= 7.900      HD= 2.283      Q= .020      T=26.00

R	U1N/UMAX	U2N/UMAX	U3N/UMAX	U4N/UMAX
.000	1.000	1.000	1.000	1.000
.166		.676		
.333		.460		
.500	.042	.217	.764	.813
1.000	.042	.048	.323	.347
1.500	.024	.048	.092	.143
2.000	.042	.048	.000	.201
2.475	.024	.000	.000	.002

HU= 8.000      HD= 2.275      Q= .014      T=26.50

R	U1N/UMAX	U2N/UMAX	U3N/UMAX	U4N/UMAX
.000	1.000	1.000	1.000	1.000
.166		.867		
.333		.509		
.500	.034	.314	.817	1.025
1.000	.000	.100	.552	.592
1.500	.000	.050	.219	.317
2.000	.000	.050	.139	.225
2.475	.000	.000	.000	.225

# THE CALCULATION OF UMN/UMAX (SERIES 2)

HU=11.800      HD= 2.523      Q= .283      T=17.50

R	U1N/UMAX	U2N/UMAX	U3N/UMAX	U4N/UMAX
.000	1.000	1.000	1.000	1.000
.166		.571	.785	.906
.333		.208	.493	.569
.500	.016	.015	.429	.508
1.000	.012	.009	.010	.176
1.500	.012	.000	-.024	-.026
2.000	.004	-.009	-.035	-.108
2.475	-.002	-.039	-.108	-.179

HU=11.960      HD= 2.519      Q= .277      T=17.50

R	U1N/UMAX	U2N/UMAX	U3N/UMAX	U4N/UMAX
.000	1.000	1.000	1.000	1.000
.166		.489	.879	.895
.333		.150	.592	.737
.500	.024	.018	.358	.495
1.000	.018	.006	.001	.116
1.500	.015	.000	-.017	-.012
2.000	.009	-.007	-.030	-.088
2.475	.000	-.045	-.117	-.233

HU=12.250      HD= 2.525      Q= .285      T=17.50

R	U1N/UMAX	U2N/UMAX	U3N/UMAX	U4N/UMAX
.000	1.000	1.000	1.000	1.000
.166		.470	.862	.884
.333		.120	.664	.760
.500	.018	.030	.305	.616
1.000	.019	.007	.007	.116
1.500	.018	.003	-.027	-.012
2.000	.015	.000	-.037	-.055
2.475	.010	-.042	-.130	-.199

HU=13.000      HD= 2.547      Q= .319      T=17.50

R	U1N/UMAX	U2N/UMAX	U3N/UMAX	U4N/UMAX
.000	1.000	1.000	1.000	1.000
.166		.507	.826	.896
.333		.086	.531	.659
.500	.020	.040	.347	.503
1.000	.026	.010	.010	.137
1.500	.020	.007	-.014	.025
2.000	.016	.002	-.014	-.001
2.475	.011	-.067	-.188	-.281

HU=13.450      HD= 2.557      Q= .333      T=17.50

R	U1N/UMAX	U2N/UMAX	U3N/UMAX	U4N/UMAX
.000	1.000	1.000	1.000	1.000
.166		.489	.732	.787
.333		.192	.373	.657
.500	.035	.069	.137	.531
1.000	.037	.026	.014	.232
1.500	.037	.018	.002	.166
2.000	.030	.009	.002	.064
2.475	.011	-.099	-.283	-.429



## THE CALCULATION OF UMN/UMAX (SERIES 3)

HU=14.870      HD= 2.620      Q= .438      T=19.80

R	U1N/UMAX	U2N/UMAX	U3N/UMAX	U4N/UMAX
.000	1.000	1.000	1.000	1.000
.166		.473	.812	.810
.333		.100	.485	.640
.500	.017	.019	.365	.371
1.000	.014	.014	-.026	.015
1.500	.014	.011	-.026	-.036
2.000	.009	.003	-.034	-.055
2.475	-.004	-.059	-.139	-.229

HU=14.620      HD= 2.611      Q= .422      T=20.00

R	U1N/UMAX	U2N/UMAX	U3N/UMAX	U4N/UMAX
.000	1.000	1.000	1.000	1.000
.166		.545	.819	.859
.333		.081	.441	.661
.500	.020	.008	.215	.434
1.000	.016	.001	-.027	.028
1.500	.014	.000	-.031	-.027
2.000	.011	-.002	-.041	-.059
2.475	.005	-.044	-.166	-.303

HU=14.790      HD= 2.610      Q= .420      T=20.40

R	U1N/UMAX	U2N/UMAX	U3N/UMAX	U4N/UMAX
.000	1.000	1.000	1.000	1.000
.166		.514	.796	.846
.333		.104	.452	.572
.500	.025	.011	.191	.430
1.000	.021	.008	-.028	.044
1.500	.020	.006	-.028	.007
2.000	.016	-.001	-.041	-.061
2.475	.001	-.042	-.199	-.304

HU=14.860      HD= 2.605      Q= .415      T=20.40

R	U1N/UMAX	U2N/UMAX	U3N/UMAX	U4N/UMAX
.000	1.000	1.000	1.000	1.000
.166		.479	.806	.885
.333		.092	.458	.645
.500	.028	.011	.185	.414
1.000	.025	.006	-.020	.051
1.500	.018	.005	-.028	.005
2.000	.014	-.003	-.055	-.014
2.475	-.000	-.078	-.230	-.281

HU=14.980      HD= 2.607      Q= .416      T=21.00

R	U1N/UMAX	U2N/UMAX	U3N/UMAX	U4N/UMAX
.000	1.000	1.000	1.000	1.000
.166		.391	.597	.850
.333		.048	.401	.569
.500	.033	.014	.066	.328
1.000	.027	.003	-.048	.067
1.500	.023	.001	-.052	.028
2.000	.015	-.014	-.064	-.069
2.475	-.007	-.108	-.362	-.633

HU=15.020      HD= 2.604      Q= .412      T=21.00

R	U1N/UMAX	U2N/UMAX	U3N/UMAX	U4N/UMAX
.000	1.000	1.000	1.000	1.000
.166		.288	.720	.706
.333		.032	.203	.508
.500	.060	.019	.040	.256
1.000	.055	.015	-.064	.159
1.500	.037	.007	-.093	.159
2.000	.031	-.022	-.112	.060
2.475	-.012	-.219	-.825	-.352

## THE CALCULATION OF UMN/UMAX (SERIES 4)

HU=22.600 HD= 2.777 Q= .728 T=21.00

R	U1N/UMAX	U2N/UMAX	U3N/UMAX	U4N/UMAX
.000	1.000	1.000	1.000	1.000
.166		.817	.946	.973
.333		.247	.668	.822
.500	.006	.037	.326	.509
1.000	.024	.018	.002	.165
1.500	.024	.006	-.039	.006
2.000	.005	-.014	-.134	-.335
2.475	-.031	-.205	-.609	-1.016

HU=22.690 HD= 2.775 Q= .725 T=21.00

R	U1N/UMAX	U2N/UMAX	U3N/UMAX	U4N/UMAX
.000	1.000	1.000	1.000	1.000
.166		.541	.859	.875
.333		.113	.628	.702
.500	.035	.042	.259	.517
1.000	.027	.017	.003	.216
1.500	.021	.015	-.078	-3.811
1.500	.021	.015	-.074	.186
2.000	.005	-.029	-.176	-.334
2.475	-.033	-.244	-.761	-1.239

HU=22.680 HD= 2.772 Q= .721 T=21.00

R	U1N/UMAX	U2N/UMAX	U3N/UMAX	U4N/UMAX
.000	1.000	1.000	1.000	1.000
.166		.387	.892	1.012
.333		.188	.419	.808
.500	.014	.030	.210	.680
1.000	.033	.035	-.052	.224
1.500	.040	.027	-.100	.132
2.000	-.005	-.065	-.306	-.366
2.475	-.078	-.315	-1.374	-2.550

HU=22.700 HD= 2.770 Q= .715 T=21.00

R	U1N/UMAX	U2N/UMAX	U3N/UMAX	U4N/UMAX
.000	1.000	1.000	1.000	1.000
.166		.214	.691	.915
.333		-.056	.140	.813
.500	.041	.023	-.243	.711
1.000	.073	.066	-.272	.504
1.500	.078	.054	-.416	.189
2.000	.021	-.132	-1.052	-2.780
2.475	-.191	-1.170	-5.878	-6.970

## C C THE STUDY OF THE CONFINED JET (3B)

THE CALCULATION OF  $U_{MAX}/U_0$  (SERIES 1)

HU= 7.500	HD= 2.299	Q= .033	T=23.00	
VALUE OF $U_{MAX}/U_0$ AT		X1	X2	X3
		1.000	.621	.302
				X4
				.135

HU= 7.700	HD= 2.295	Q= .030	T=24.00	
VALUE OF $U_{MAX}/U_0$ AT		X1	X2	X3
		1.000	.628	.285
				X4
				.130

HU= 7.820	HD= 2.289	Q= .024	T=25.10	
VALUE OF $U_{MAX}/U_0$ AT		X1	X2	X3
		1.000	.699	.313
				X4
				.163

HU= 7.900	HD= 2.283	Q= .020	T=26.00	
VALUE OF $U_{MAX}/U_0$ AT		X1	X2	X3
		1.000	.687	.351
				X4
				.165

HU= 8.000	HD= 2.275	Q= .014	T=26.50	
VALUE OF $U_{MAX}/U_0$ AT		X1	X2	X3
		1.000	.667	.331
				X4
				.149

THE CALCULATION OF  $U_{MAX}/U_0$  (SERIES 2)

HU=11.800	HD= 2.523	Q= .283	T=17.50	
VALUE OF $U_{MAX}/U_0$ AT		X1	X2	X3
		1.000	.653	.382
				X4
				.227

HU=11.960	HD= 2.519	Q= .277	T=17.50	
VALUE OF $U_{MAX}/U_0$ AT		X1	X2	X3
		1.000	.663	.371
				X4
				.220

HU=12.250	HD= 2.525	Q= .285	T=17.50	
VALUE OF $U_{MAX}/U_0$ AT		X1	X2	X3
		1.000	.623	.398
				X4
				.236

HU=13.000	HD= 2.547	Q= .319	T=17.50	
VALUE OF UMAX/UO AT		X1	X2	X3
		1.000	.611	.384
				X4
				.244

HU=13.450	HD= 2.557	Q= .333	T=17.50	
VALUE OF UMAX/UO AT		X1	X2	X3
		1.000	.576	.367
				X4
				.203

# THE CALCULATION OF UMAX/UO (SERIES 3)

HU=14.870	HD= 2.620	Q= .438	T=19.80	
VALUE OF UMAX/UO AT		X1	X2	X3
		1.000	.694	.369
				X4
				.235

HU=14.620	HD= 2.611	Q= .422	T=20.00	
VALUE OF UMAX/UO AT		X1	X2	X3
		1.000	.687	.365
				X4
				.232

HU=14.790	HD= 2.610	Q= .420	T=20.40	
VALUE OF UMAX/UO AT		X1	X2	X3
		1.000	.676	.364
				X4
				.220

HU=14.860	HD= 2.605	Q= .415	T=20.40	
VALUE OF UMAX/UO AT		X1	X2	X3
		1.000	.647	.362
				X4
				.212

HU=14.980	HD= 2.607	Q= .416	T=21.00	
VALUE OF UMAX/UO AT		X1	X2	X3
		1.000	.646	.349
				X4
				.173

HU=15.020	HD= 2.604	Q= .412	T=21.00	
VALUE OF UMAX/UO AT		X1	X2	X3
		1.000	.630	.263
				X4
				.156

THE CALCULATION OF  $U_{MAX}/U_0$  (SERIES 4)

HU=22.600	HD= 2.777	Q= .728	T=21.00	
VALUE OF $U_{MAX}/U_0$ AT		X1	X2	X3
		1.000	.678	.326
				X4
				.187

HU=22.690	HD= 2.775	Q= .725	T=21.00	
VALUE OF $U_{MAX}/U_0$ AT		X1	X2	X3
		1.000	.626	.300
				X4
				.182

HU=22.680	HD= 2.772	Q= .721	T=21.00	
VALUE OF $U_{MAX}/U_0$ AT		X1	X2	X3
		1.000	.583	.260
				X4
				.141

HU=22.700	HD= 2.770	Q= .715	T=21.00	
VALUE OF $U_{MAX}/U_0$ AT		X1	X2	X3
		1.000	.487	.129
				X4
				.109

## C C THE STUDY OF THE CONFINED JET (4B)

THE CALCULATION OF  $UMN/U_0$  (SERIES 1)

HU= 7.500      HD= 2.299      Q= .033      T=23.00

R	U1N/U0	U2N/U0	U3N/U0	U4N/U0
.000	1.000	.621	.302	.135
.166		.549	.284	
.333		.339	.272	
.500	.041	.187	.231	.124
1.000	.025	.028	.107	.077
1.500	.021	.025	.000	.029
2.000	.021	.020	.044	.043
2.475	.000	.028	.000	.020

HU= 7.700      HD= 2.295      Q= .030      T=24.00

R	U1N/U0	U2N/U0	U3N/U0	U4N/U0
.000	1.000	.628	.285	.130
.166		.549	.277	
.333		.351	.252	
.500	.033	.177	.213	.115
1.000	.023	.027	.099	.076
1.500	.025	.022	-.000	.045
2.000	.023	.021	.034	.039
2.475	.023	.035	.015	.022

HU= 7.820      HD= 2.289      Q= .024      T=25.10

R	U1N/U0	U2N/U0	U3N/U0	U4N/U0
.000	1.000	.699	.313	.163
.166		.523	.296	
.333		.277	.280	
.500	.057	.164	.231	.123
1.000	.049	.028	.095	.076
1.500	.040	.000	.033	.028
2.000	.049	.028	.033	.039
2.475	.040	.044	.000	.000

HU= 7.900      HD= 2.283      Q= .020      T=26.00

R	U1N/U0	U2N/U0	U3N/U0	U4N/U0
.000	1.000	.687	.351	.165
.166		.464		
.333		.316		
.500	.042	.149	.268	.134
1.000	.042	.033	.113	.057
1.500	.024	.033	.032	.024
2.000	.042	.031	.000	.033
2.475	.024	.000	.000	.000

HU= 8.000      HD= 2.275      Q= .014      T=26.50

R	U1N/U0	U2N/U0	U3N/U0	U4N/U0
.000	1.000	.667	.331	.149
.166		.579		
.333		.340		
.500	.034	.210	.270	.153
1.000	.000	.066	.183	.088
1.500	.000	.033	.072	.047
2.000	.000	.033	.046	.034
2.475	.000	.000	.000	.034

# THE CALCULATION OF UMN/U0 (SERIES 2)

HU=11.800      HD= 2.523      Q= .283      T=17.50

R	U1N/U0	U2N/U0	U3N/U0	U4N/U0
.000	1.000	.653	.382	.227
.166		.373	.300	.206
.333		.136	.188	.129
.500	.016	.010	.164	.115
1.000	.012	.006	.004	.040
1.500	.012	.000	-.009	-.006
2.000	.004	-.006	-.014	-.025
2.475	-.002	-.025	-.041	-.041



HU=11.960      HD= 2.519      Q= .277      T=17.50

R	U1N/U0	U2N/U0	U3N/U0	U4N/U0
.000	1.000	.663	.371	.220
.166		.325	.327	.197
.333		.099	.220	.162
.500	.024	.012	.133	.109
1.000	.018	.004	.000	.025
1.500	.015	.000	-.006	-.003
2.000	.009	-.005	-.011	-.019
2.475	.000	-.030	-.044	-.051

HU=12.250      HD= 2.525      Q= .285      T=17.50

R	U1N/U0	U2N/U0	U3N/U0	U4N/U0
.000	1.000	.623	.398	.236
.166		.293	.343	.208
.333		.075	.264	.179
.500	.018	.019	.121	.145
1.000	.015	.004	.003	.027
1.500	.018	.002	-.011	-.003
2.000	.015	.000	-.015	-.013
2.475	.010	-.026	-.052	-.047

HU=13.000      HD= 2.547      Q= .319      T=17.50

R	U1N/U0	U2N/U0	U3N/U0	U4N/U0
.000	1.000	.611	.384	.244
.166		.309	.317	.218
.333		.053	.204	.161
.500	.020	.024	.133	.123
1.000	.026	.006	.004	.033
1.500	.020	.004	-.005	.006
2.000	.016	.001	-.005	-.000
2.475	.011	-.041	-.072	-.068

HU=13.450      HD= 2.557      Q= .333      T=17.50

R	U1N/U0	U2N/U0	U3N/U0	U4N/U0
.000	1.000	.576	.367	.203
.166		.282	.269	.160
.333		.111	.137	.134
.500	.035	.040	.050	.108
1.000	.037	.015	.005	.047
1.500	.037	.010	.000	.034
2.000	.030	.005	.000	.013
2.475	.011	-.057	-.104	-.087

THE CALCULATION OF  $UMN/UO$  (SERIES 3)

HU=14.870      HD= 2.620      Q= .438      T=19.80

R	U1N/UO	U2N/UO	U3N/UO	U4N/UO
.000	1.000	.694	.369	.235
.166		.328	.300	.190
.333		.069	.179	.150
.500	.017	.014	.135	.087
1.000	.014	.009	-.010	.003
1.500	.014	.008	-.010	-.008
2.000	.009	.002	-.013	-.013
2.475	-.004	-.041	-.051	-.054

HU=14.620      HD= 2.611      Q= .422      T=20.00

R	U1N/UO	U2N/UO	U3N/UO	U4N/UO
.000	1.000	.687	.365	.232
.166		.374	.299	.200
.333		.056	.161	.154
.500	.020	.005	.078	.101
1.000	.016	.001	-.010	.006
1.500	.014	.000	-.011	-.006
2.000	.011	-.001	-.015	-.014
2.475	.005	-.030	-.061	-.070

HU=14.790      HD= 2.610      Q= .420      T=20.40

R	U1N/UO	U2N/UO	U3N/UO	U4N/UO
.000	1.000	.676	.364	.220
.166		.348	.289	.187
.333		.070	.165	.126
.500	.025	.007	.069	.095
1.000	.021	.006	-.010	.010
1.500	.020	.004	-.010	.002
2.000	.016	-.000	-.015	-.014
2.475	.001	-.028	-.073	-.067

HU=14.860      HD= 2.605      Q= .415      T=20.40

R	U1N/U0	U2N/U0	U3N/U0	U4N/U0
.000	1.000	.647	.362	.212
.166		.310	.292	.187
.333		.060	.166	.137
.500	.028	.007	.067	.088
1.000	.025	.004	-.007	.011
1.500	.018	.003	-.010	.001
2.000	.014	-.002	-.020	-.003
2.475	-.000	-.050	-.083	-.059

HU=14.980      HD= 2.607      Q= .416      T=21.00

R	U1N/U0	U2N/U0	U3N/U0	U4N/U0
.000	1.000	.646	.349	.173
.166		.253	.208	.147
.333		.031	.140	.098
.500	.033	.009	.023	.057
1.000	.027	.002	-.017	.012
1.500	.023	.000	-.018	.005
2.000	.015	-.009	-.022	-.012
2.475	-.007	-.070	-.126	-.110

HU=15.020      HD= 2.604      Q= .412      T=21.00

R	U1N/U0	U2N/U0	U3N/U0	U4N/U0
.000	1.000	.630	.263	.156
.166		.182	.189	.111
.333		.020	.053	.080
.500	.060	.012	.010	.040
1.000	.055	.010	-.017	.025
1.500	.037	.004	-.024	.025
2.000	.031	-.014	-.029	.009
2.475	-.012	-.138	-.217	-.055

## THE CALCULATION OF UMN/UO (SERIES 4)

HU=22.600      HD= 2.777      Q= .728      T=21.00

R	U1N/UO	U2N/UO	U3N/UO	U4N/UO
.000	1.000	.678	.326	.187
.166		.554	.308	.182
.333		.168	.218	.154
.500	.006	.025	.106	.095
1.000	.024	.012	.000	.031
1.500	.024	.004	-.013	.001
2.000	.005	-.009	-.044	-.063
2.475	-.031	-.139	-.199	-.190

HU=22.690      HD= 2.775      Q= .725      T=21.00

R	U1N/UO	U2N/UO	U3N/UO	U4N/UO
.000	1.000	.626	.300	.182
.166		.339	.258	.159
.333		.071	.189	.128
.500	.035	.026	.078	.094
1.000	.027	.011	.000	.039
1.500	.021	.009	-.023	-.692
1.500	.021	.009	-.022	.034
2.000	.005	-.018	-.053	-.061
2.475	-.033	-.153	-.229	-.225

HU=22.680      HD= 2.772      Q= .721      T=21.00

R	U1N/UO	U2N/UO	U3N/UO	U4N/UO
.000	1.000	.583	.260	.141
.166		.226	.232	.142
.333		.109	.109	.114
.500	.014	.018	.055	.096
1.000	.033	.020	-.013	.032
1.500	.040	.016	-.026	.019
2.000	-.005	-.038	-.080	-.052
2.475	-.078	-.184	-.358	-.359

HU=22.700      HD= 2.770      Q= .715      T=21.00

R	U1N/UO	U2N/UO	U3N/UO	U4N/UO
.000	1.000	.487	.129	.109
.166		.104	.089	.099
.333		-.027	.018	.088
.500	.041	.011	-.031	.077
1.000	.073	.032	-.035	.055
1.500	.078	.026	-.054	.021
2.000	.021	-.064	-.135	-.302
2.475	-.191	-.570	-.756	-.758

INVESTIGATIONS OF THE AXISYMMETRICAL  
CONFINED JET

by

Wen-shiuh Hwang

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AN ABSTRACT OF A THESIS

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The difference in velocity between a jet and the region into which it is discharged will give rise to a pronounced degree of instability, the kinetic energy of the oncoming flow steadily being converted into kinetic energy of turbulence and the later steadily decaying through viscous shear.

The purpose of this thesis is to observe the above phenomena in a confined jet. The study of this type of jet has been based on the condition of continuity rather than the constancy of momentum flux and has been analysed by the introduction of some dimensionless groups.

For a confined jet without a secondary flow, there will be recirculation occurring within the region outside of the jet. For the case of a jet with a moving secondary flow, the recirculation will disappear. The velocity in the region outside the diffusion zone will be reduced by some amount which is dependent on the magnitude of the difference of the velocities of the two streams.

The experimental results obtained show that the process of mixing will be completed within a determinable distance downstream of the jet. The maximum velocity along the central axis of the jet will approach a constant value as the flow continues downstream.

This investigation indicates that the Gaussian function method used in the study of a free jet is inadequate for the treatment of the confined jet. However, the introduction of dimensionless groups provides a very good solution.